

# NiCT *EXAT2008*

## Optical Orthogonal Frequency Division Multiplexing: the story so far....

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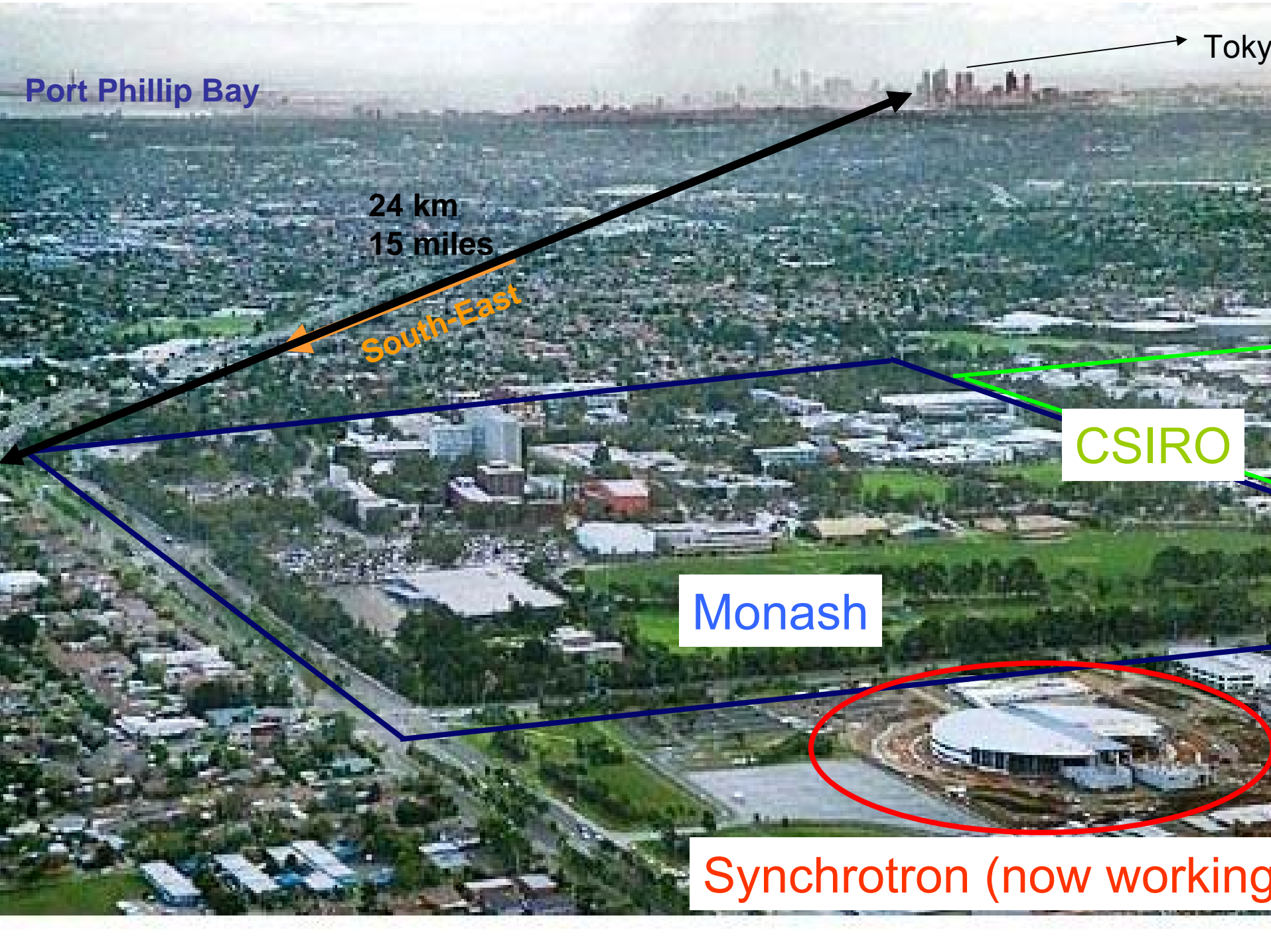
# NiCT *EXAT2008*

## Abstract

OFDM is well known to provide significant benefits to wireless transmission, but has only recently been accepted into the optical communications community.

Over the last 2 years many different optical OFDM schemes have been proposed, simulated and demonstrated experimentally; O-OFDM is now seen as a potential 100 Gbit/s technology, providing high spectral efficiency and in-built dispersion and nonlinearity compensation.

This talk will cover the background to optical OFDM, some of the issues that at first made it unattractive, and the solutions to these issues proposed by various groups.



Port Phillip Bay

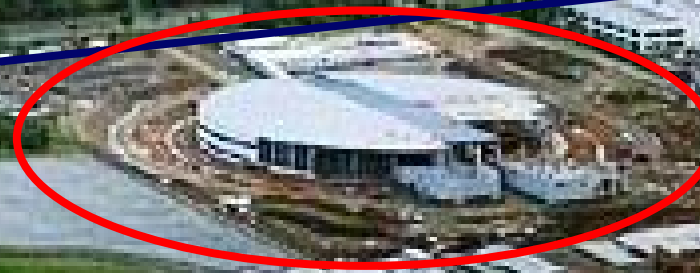
Tokyo

24 km  
15 miles

South-East

CSIRO

Monash



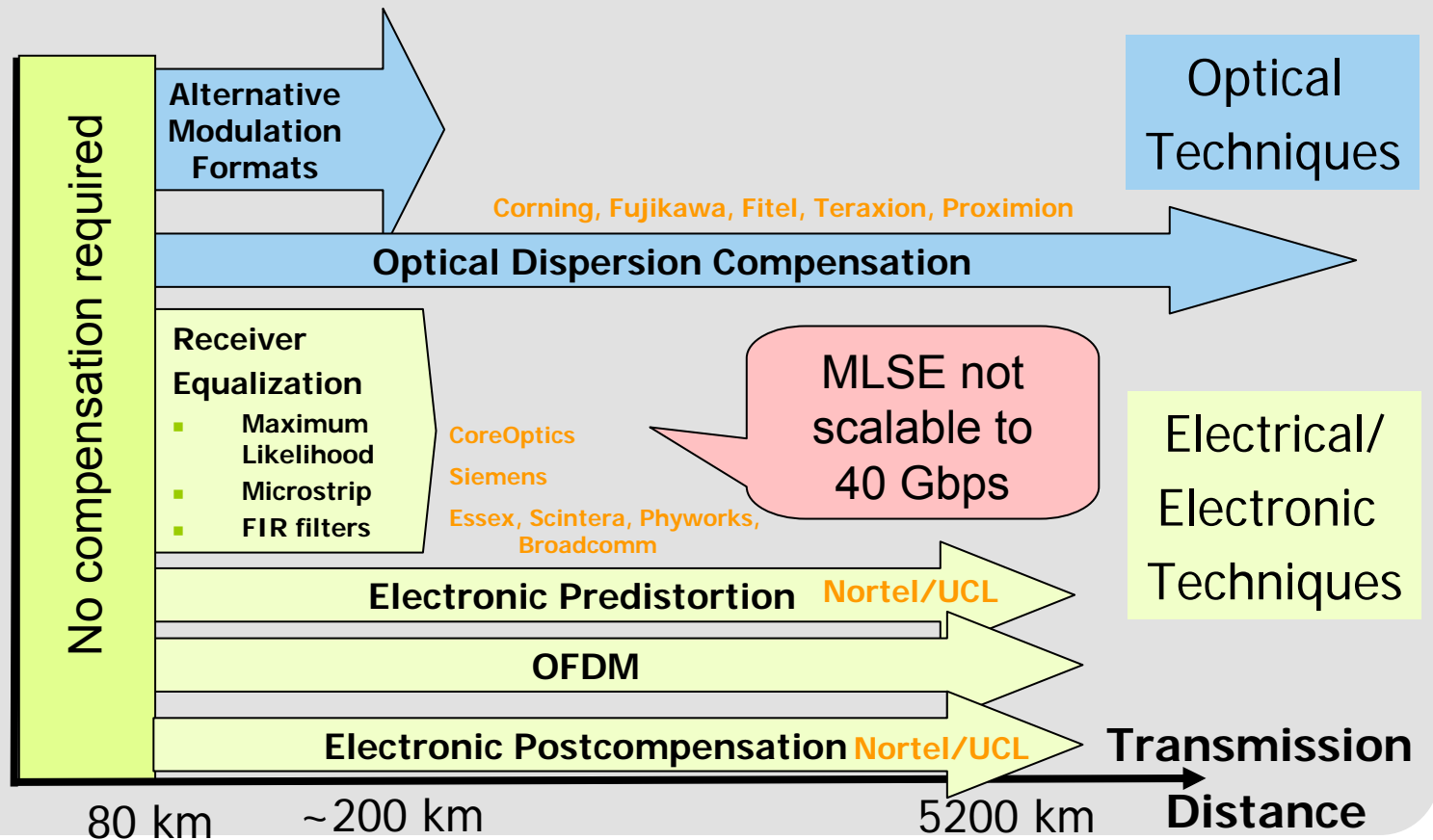
Synchrotron (now working)

# Summary

- Electronic Dispersion Compensation
- Flavors of Orthogonal Frequency Division Multiplexing
- Principle of OFDM
- OFDM for Long-Haul
- Experimental Results
  - 10 Gbit/s 4-QAM RF Unconverted
  - 20 Gbit/s Direct Digital Synthesis
  - 24 Gbit/s Colorless transmitter (2008 design)
- Nonlinearity Effects and Compensation
- Scaling to higher bit rates
- Conclusions

# The Dispersion Limit

10 Gbit/s/wavelength

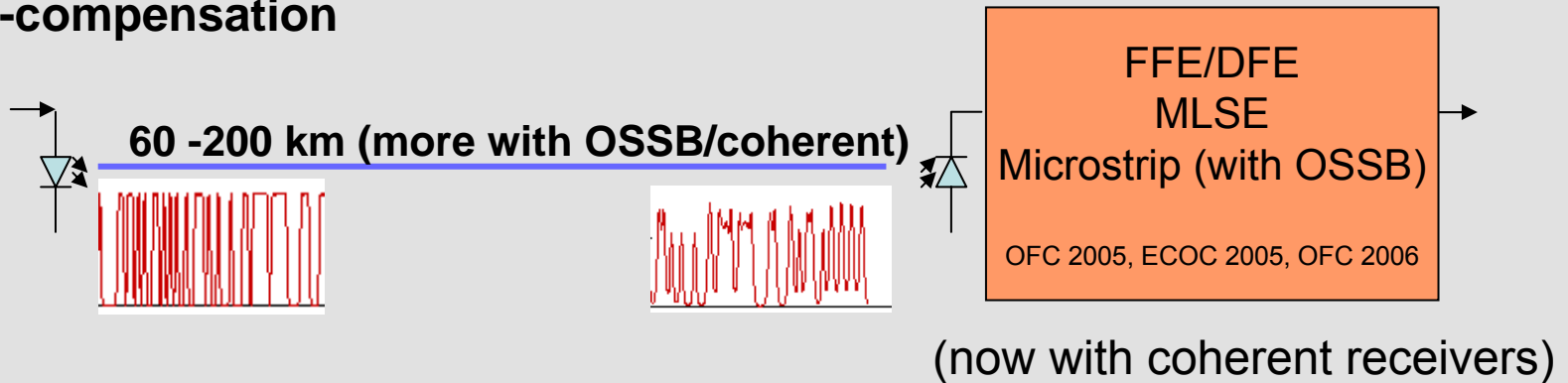


# Electronic Dispersion Compensation (EDC)

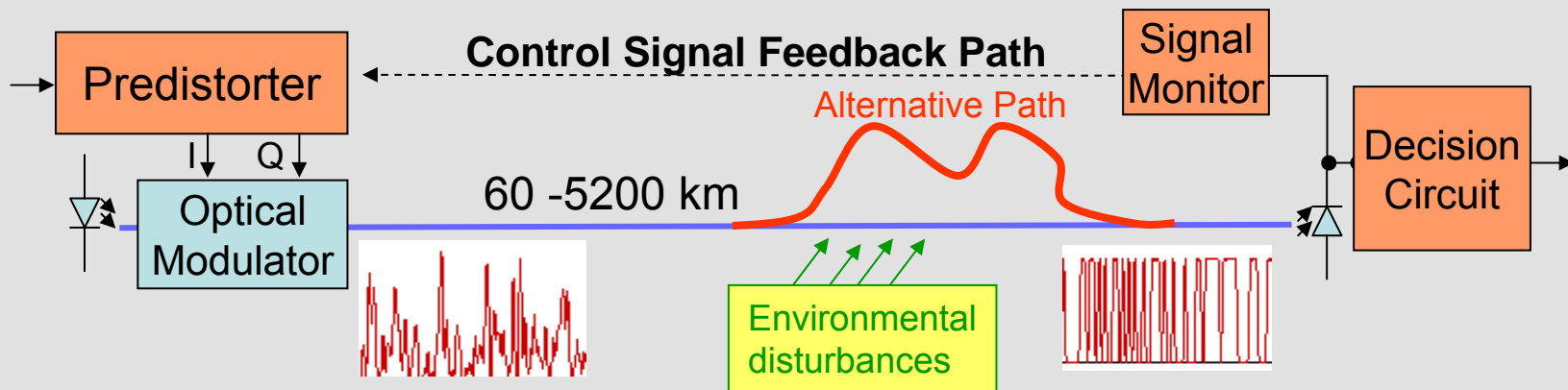
- Replaces optics with electronics
  - CMOS is cheap and gets better by the year
  - Software/Firmware is easily upgradable
- Advantages
  - Complexity at the ends of a link (edges of a network)
  - “Plug and Play” – reduced link engineering
  - Reduces outside plant (amplifiers and dispersion compensators)
  - Could support rapidly changing network topologies
  - Reduces the risk that a network wont work
  - No clock recovery issues
  - Efficient numerical computation, even at 40 Gbps
  - Identifies causes of degradation (self monitoring)

# Two Common Types of EDC

## Post-compensation



## Pre-compensation D. McGhan *et al.* OFC2005.



# OFDM

## Introduction to Theory

For an up-to-date list of publications, type “Arthur Lowery” into Google

# Orthogonal Frequency Division Multiplexing

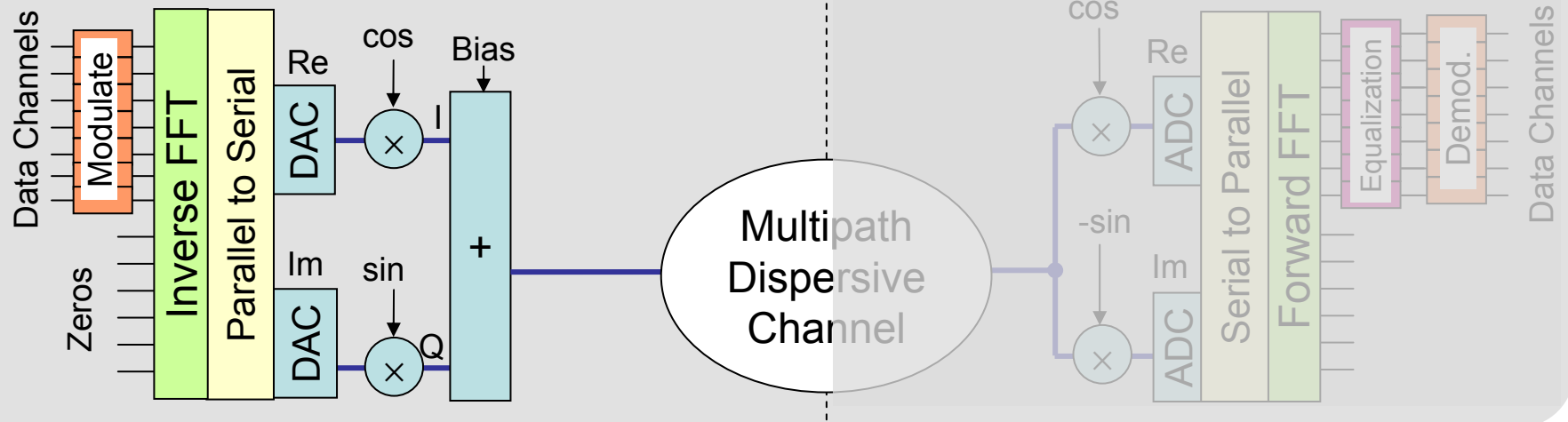
- Uses many narrow-bandwidth channels
  - Each is tolerant to dispersion (almost infinite dispersion limit)
  - Generated using an **inverse** Fast Fourier Transform
  - Separated using a Fast Fourier Transform
- Used for digital broadcasting, wireless, next generation mobile, ADSL
  - Already accepted as the best solution for radio channels
- Scalable to high bit rates (Processing  $\approx n \log_2 n$ )

# Typical OFDM System: Transmitter

Generates high numbers of subcarriers each carrying one QAM symbol

- Modulators take parallel channels
- IFFT generates OFDM waveform
  - zeros give polynomial interpolation
- DACs and I-Q modulators create real-valued waveform (OFDM band)

- I-Q demodulators and ADCs create complex waveform
- FFT separates subcarriers
- Equalizer corrects phase & amplitude
- Demodulators extract binary data

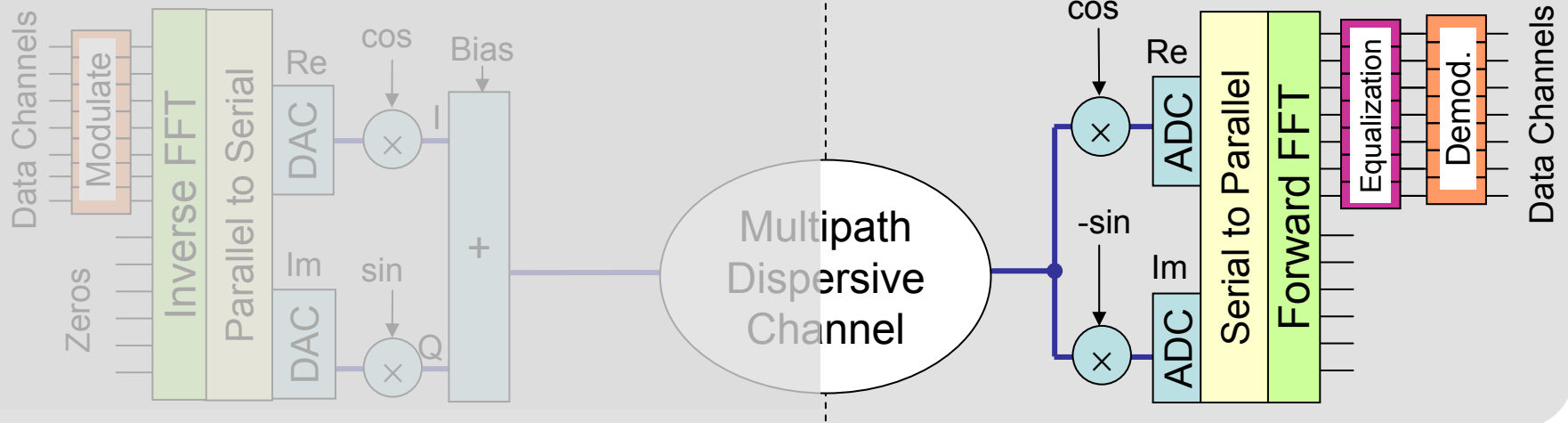


# Typical OFDM System: Receiver

Generates high numbers of subcarriers each carrying one QAM symbol

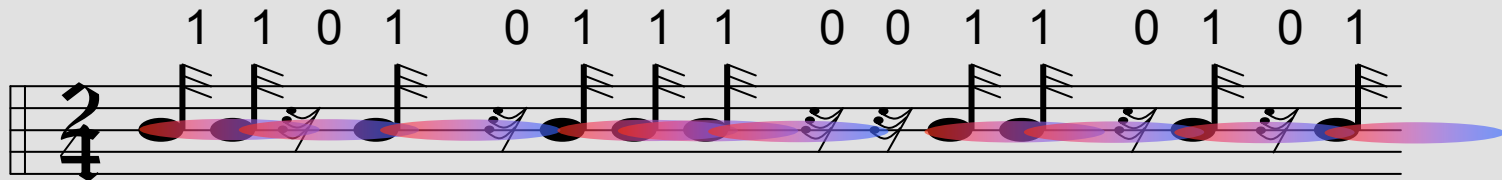
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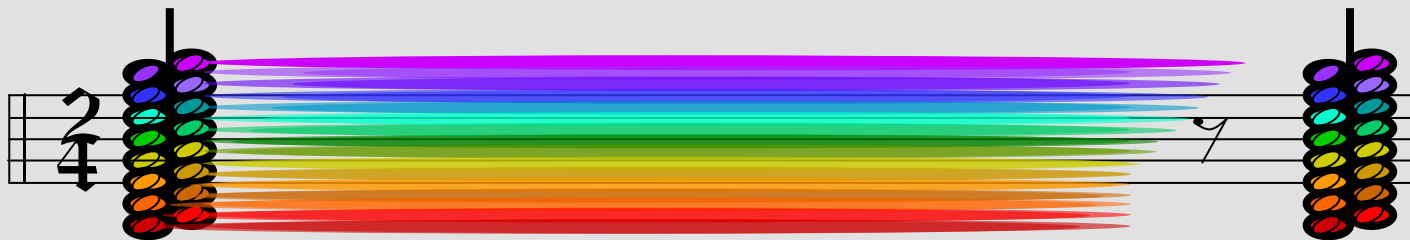


# Principle of OFDM – Music Analogy

- Conventional systems transmit on a single frequency, using a ‘beat’ for a ‘1’ and a space for a ‘0’.
- Dispersion causes their energy to spread into adjacent beats.

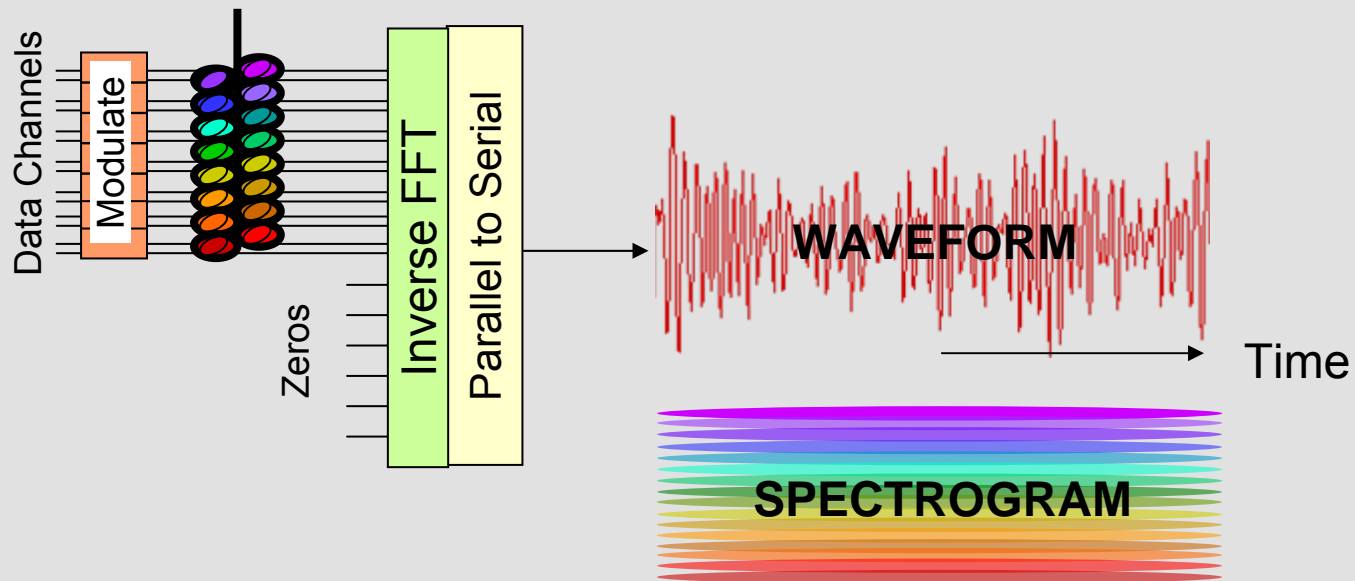


- OFDM transmits many parallel frequencies (*notes*) simultaneously (a musical chord), held for a long time
- The information is in the complexity of the ‘chord’
- Dispersion can be handled by Guard bands or Cyclic Prefixes



# Generating the Subcarriers (Transmitter)

- An Inverse Fast Fourier Transform is an easy way to generate the waveform from a superposition of subcarriers



- Usually QAM modulation is used to set the phase and amplitude of each subcarrier
- The iFFT can be stuffed with zeros to give a higher sample rate (better defined spectrum with aliasing away from main band)

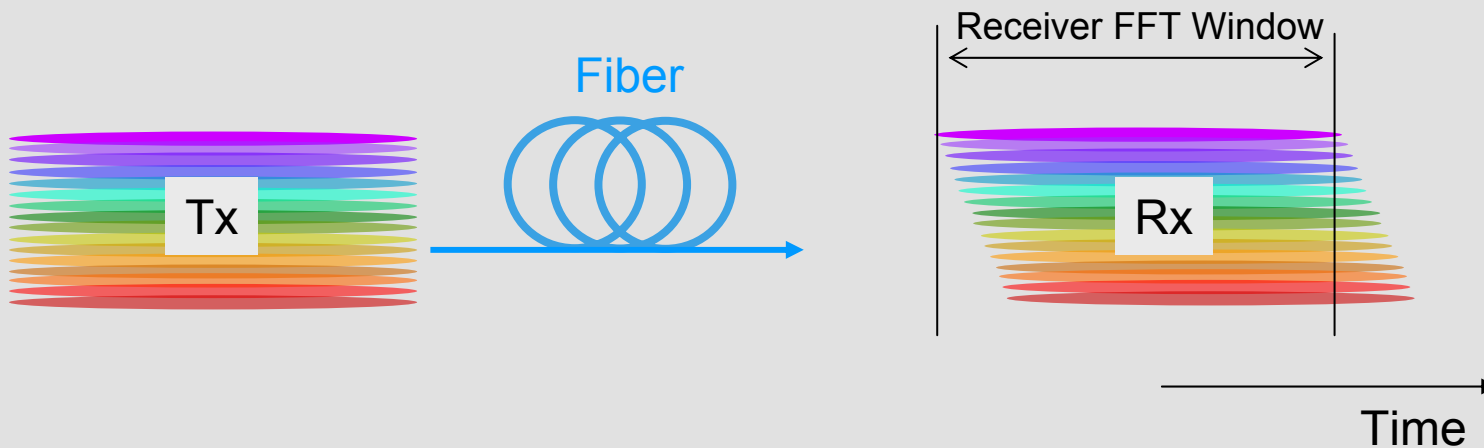
# OFDM

## Equalising Dispersion

# Dispersion 1

Dispersion delays **redder** subcarriers compared with **bluer** subcarriers

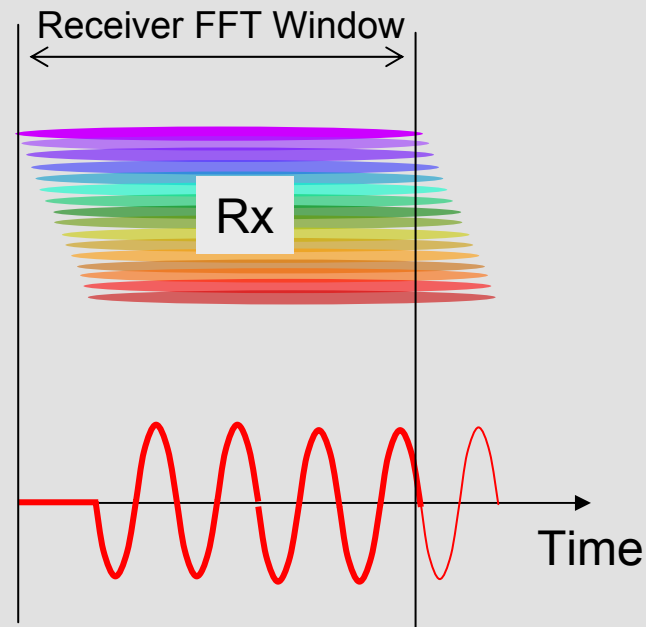
- consider the reddest subcarrier shifted out of the receiver FFT window...



# Dispersion 2

Dispersion delays **redder** subcarriers compared with **bluer** subcarriers

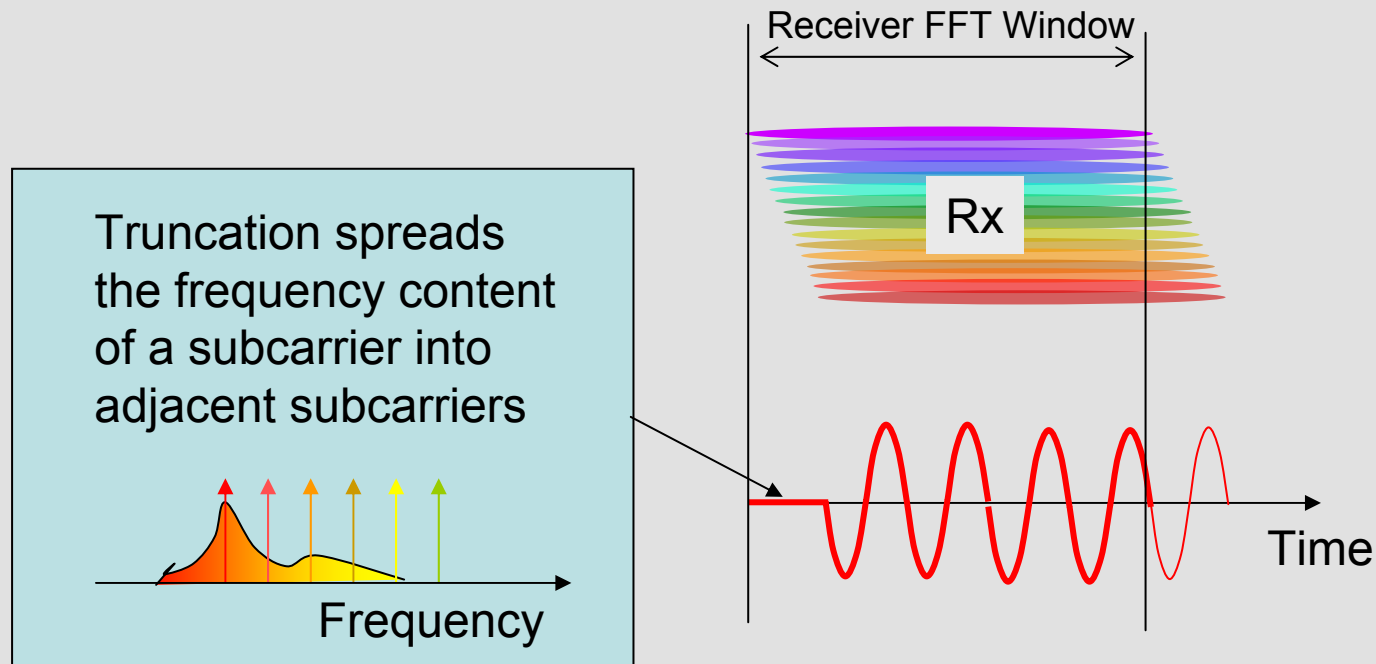
- consider the reddest subcarrier shifted out of the receiver FFT window...



# Dispersion 3

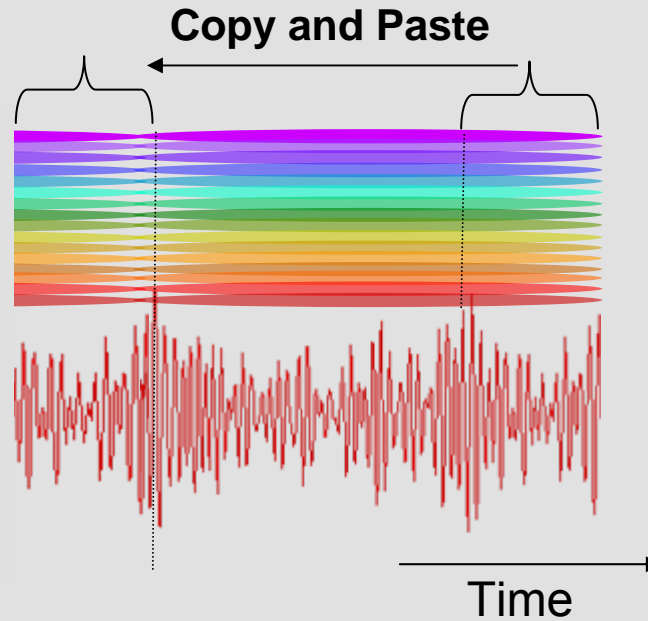
Dispersion delays **redder** subcarriers compared with **bluer** subcarriers

- consider the reddest subcarrier shifted out of the receiver FFT window...



# Cyclic Prefix 1

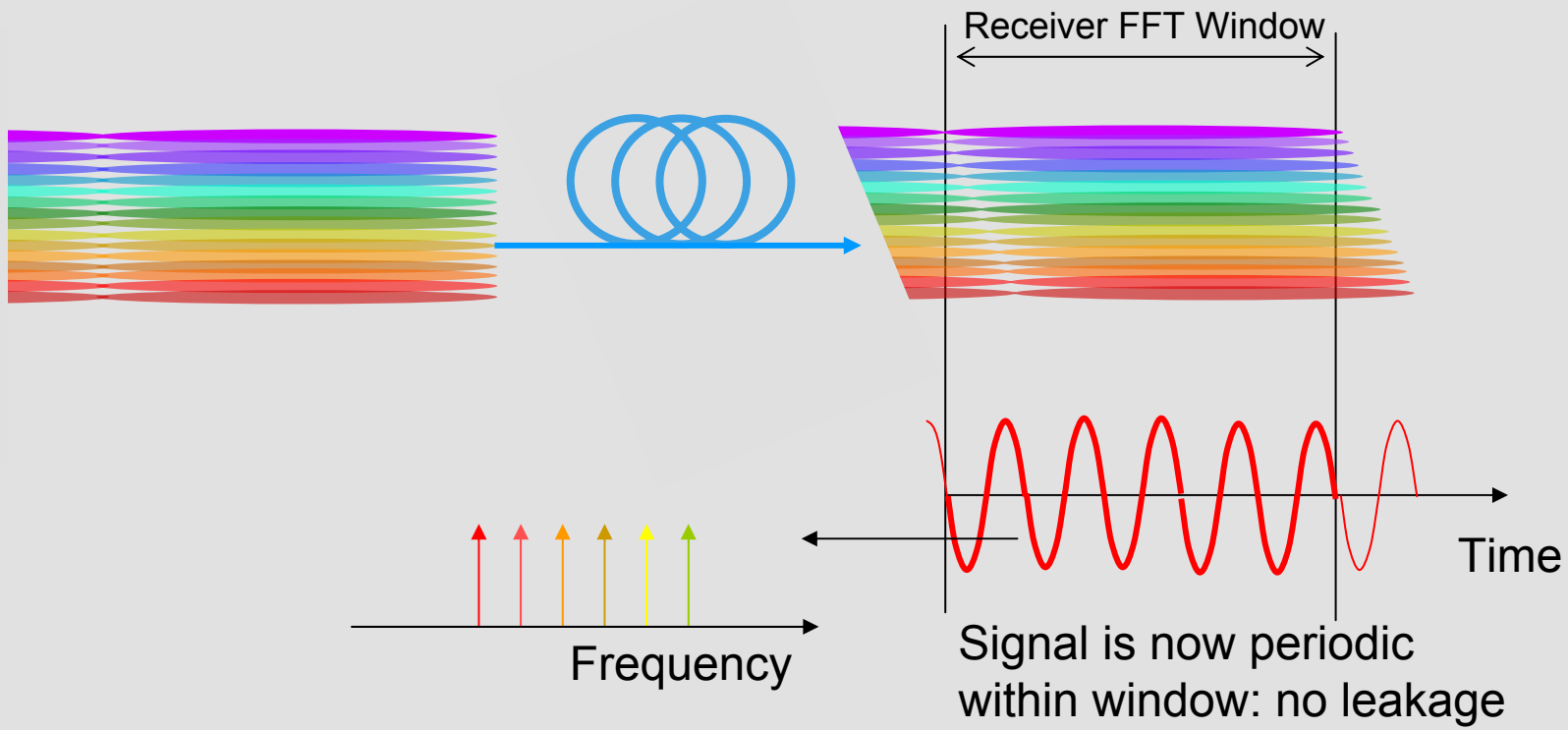
To cope with dispersion delaying each signal differently, a **cyclic prefix** is added to the signal before transmission



The duration of the prefix is equal to the differential delay across the signal's bandwidth. This is a small fraction of the length of the OFDM symbol.

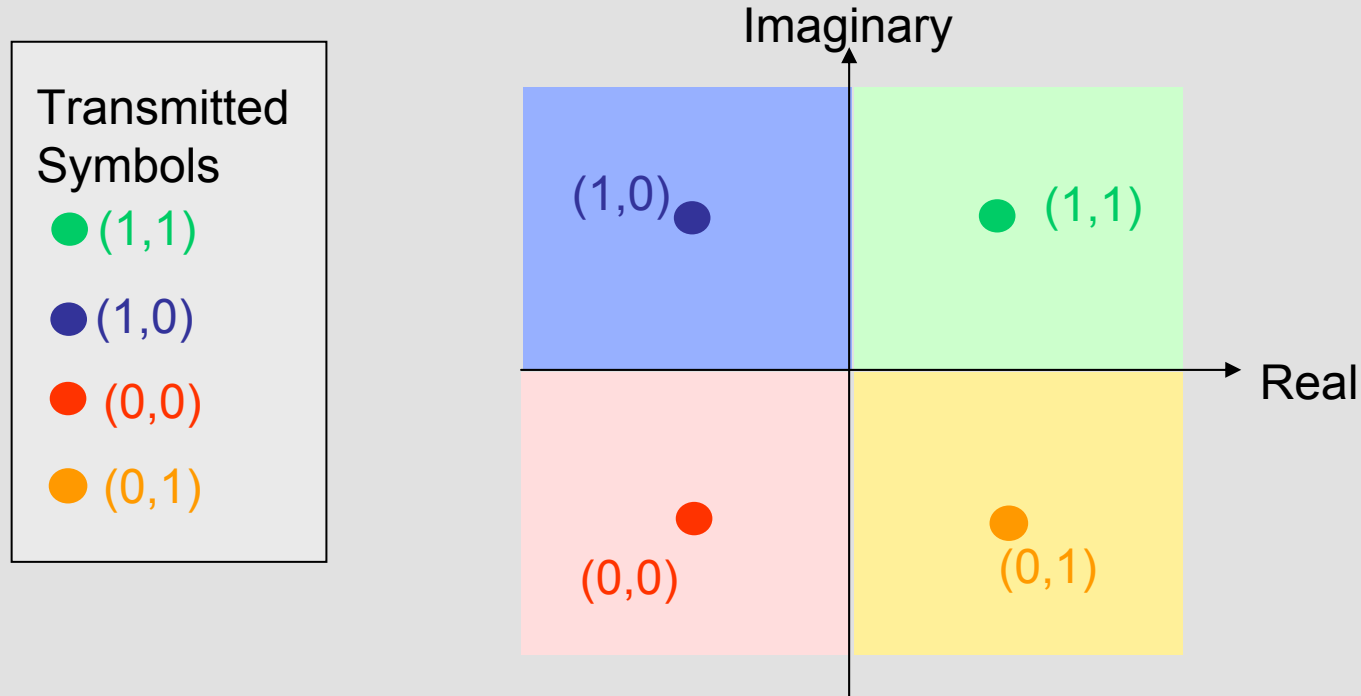
# Cyclic Prefix 2

- The cyclic prefix ensures identical signals are shifted into the FFT window, as are shifted out



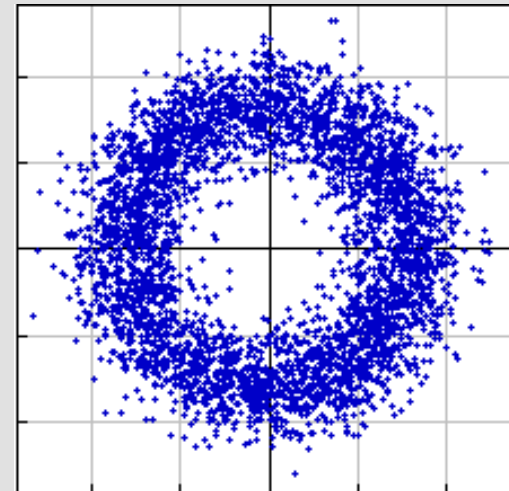
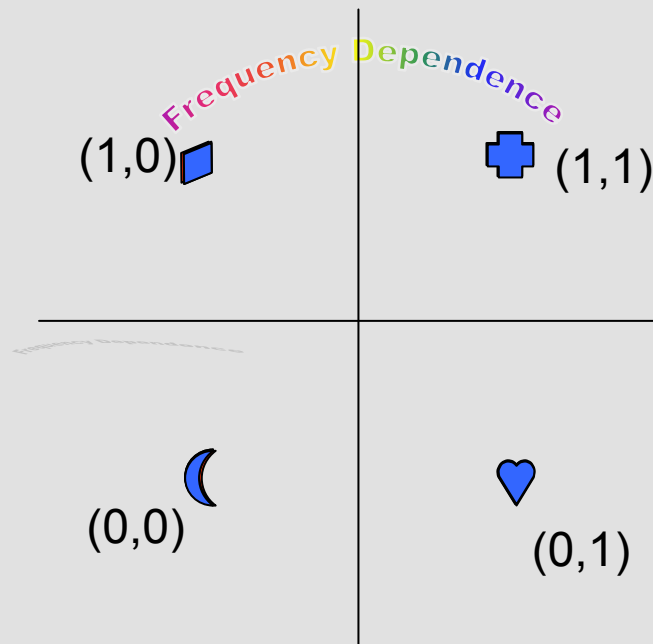
# Equalization 1

- In 4-QAM, data is encoded onto the phase
- A symbol will be received without error if it falls in the correct quadrant in phase space



# Equalization 2

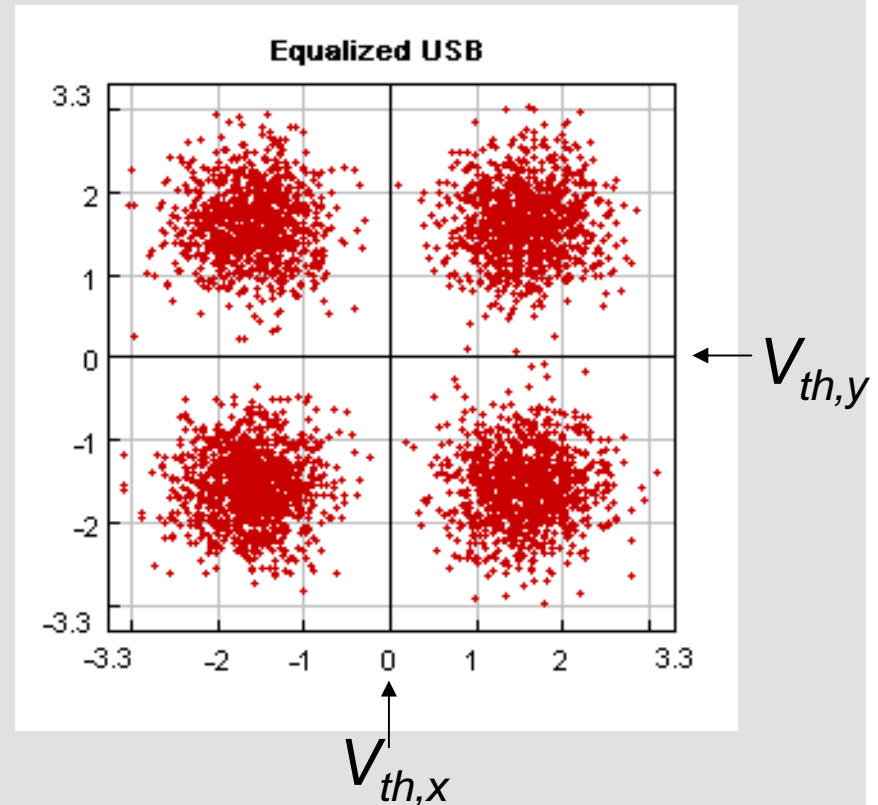
- Dispersion shifts the phases of the subcarriers dependent on their frequency
- A >45-degree phase shift causes an error



Noise also spreads the positions of symbols

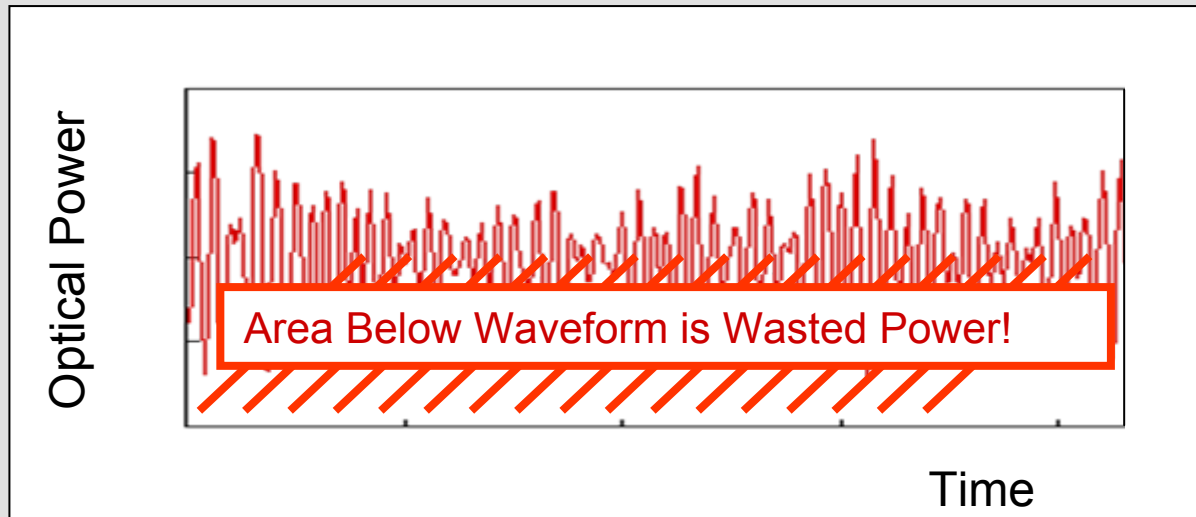
# Equalization 3

- Equalization 'unwinds' the phase distortion, placing the received symbols in the correct quadrants
  - noise and FWM will cause errors
- Equalization relies on training symbols or pilot tones within a symbol
  - this causes an overhead, reducing data rate
- Coherent systems require frequent equalization because of the evolving relative phases of the transmitter oscillator and local oscillator



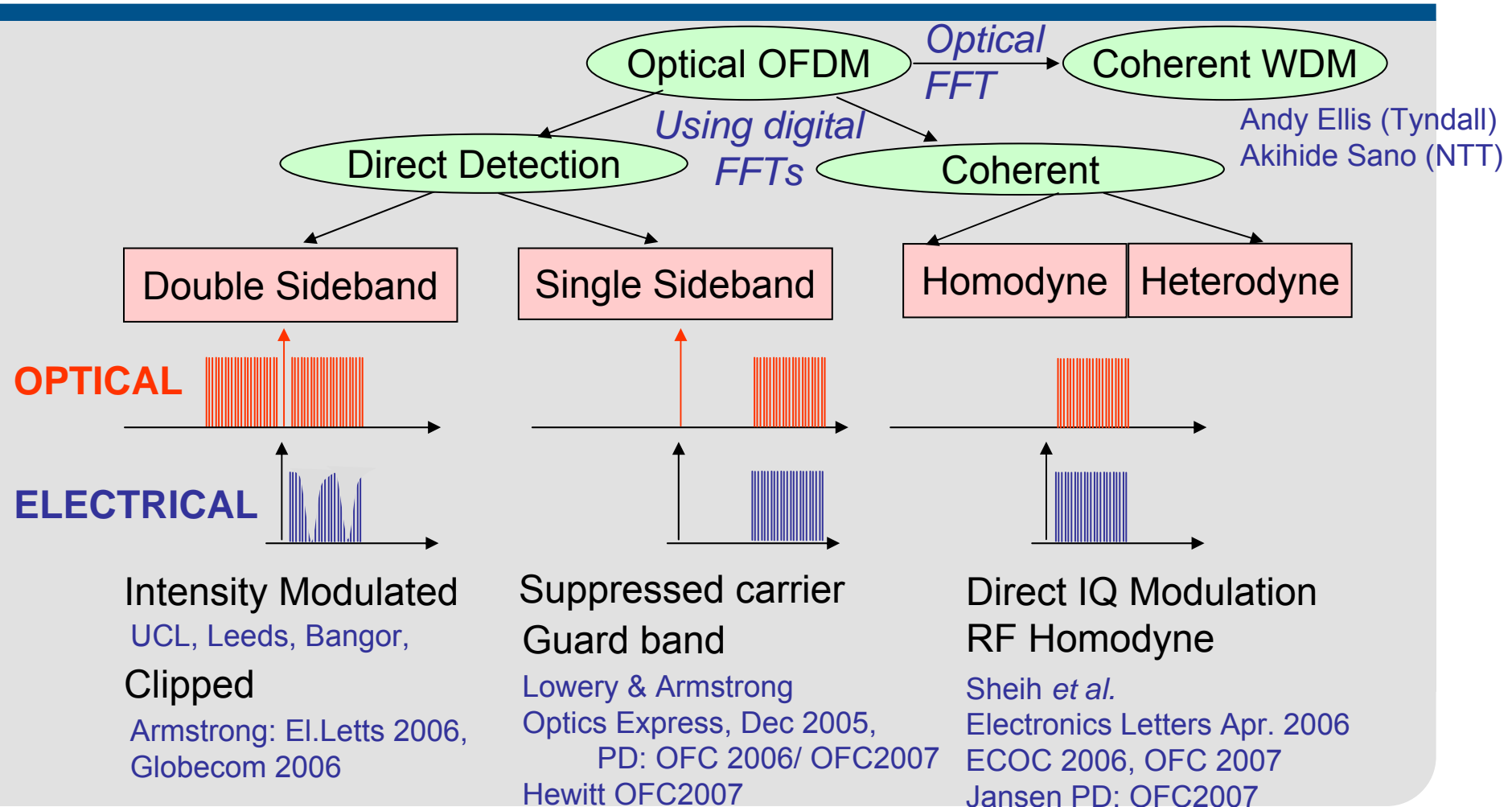
# OFDM for Optical - Issues

- Bipolar Signal - requires high bias – high mean power



- Requires Optical Single Sideband Transmission
  - To remove nulls in the baseband (RF) response
- Sensitive to optical fiber nonlinearities
- Sensitive to intermodulation distortion (e.g. square-law detection)

# Flavors of OFDM



# Our Solution at Monash

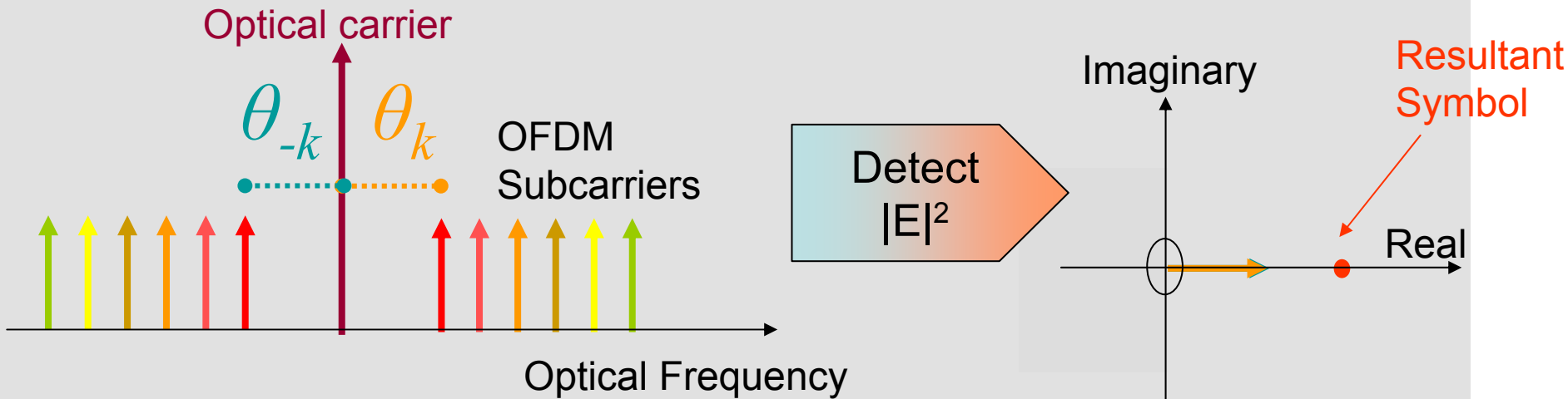
- Direct-Detection
- Single-Sideband
- Carrier Suppression
- Guard-band

With:

- Nonlinearity pre- and post- compensation
- Carrier Boost

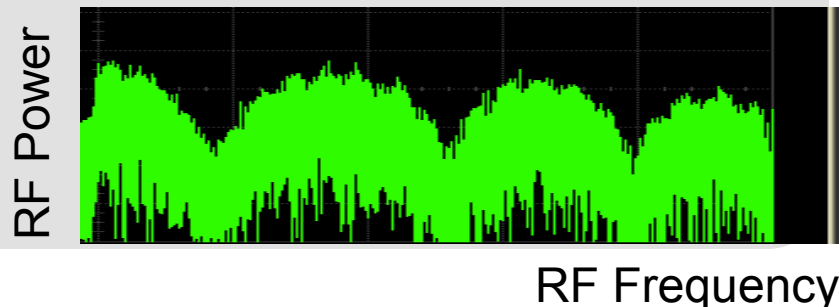
Details in J. Lightwave Technology, Jan 2008  
(Schmidt, Lowery, Armstrong)

# Why Optical Single Sideband? (1)

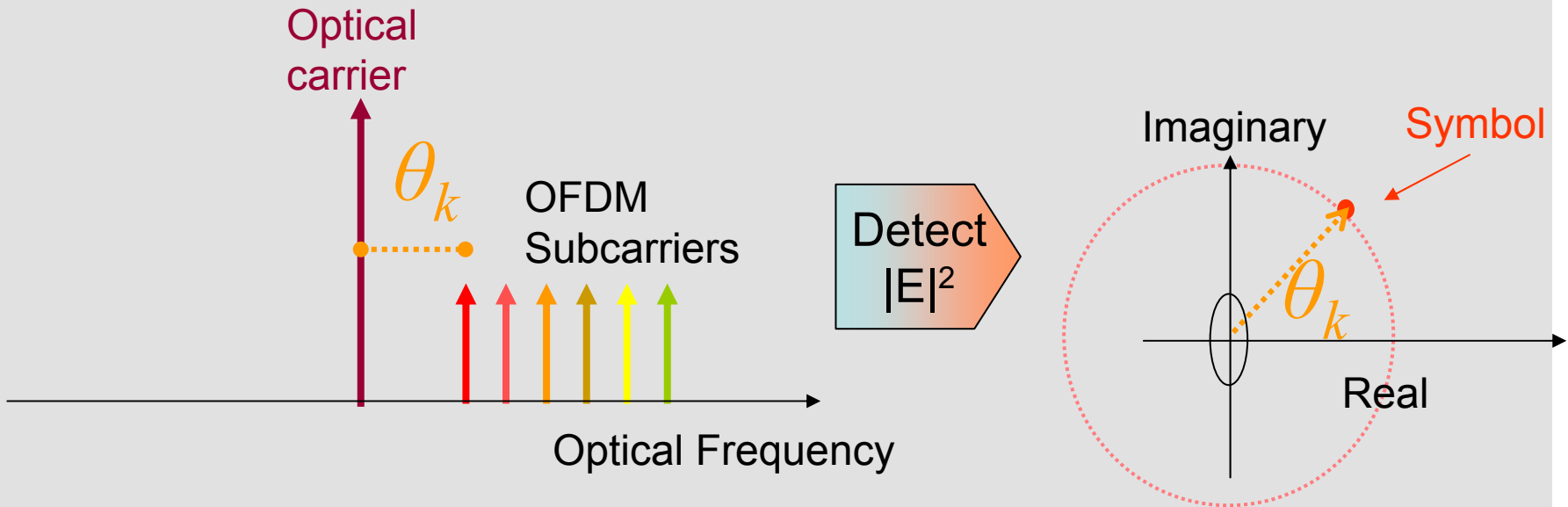


1) Consider the phase shifts of the upper and lower sidebands due to dispersion (relative to the carrier)

- 2) Symbol always lies on the real axis.
- 3) Phase shifts of  $(n+1)\pi/2$  null the subcarrier power.



# Why Optical Single Sideband? (2)

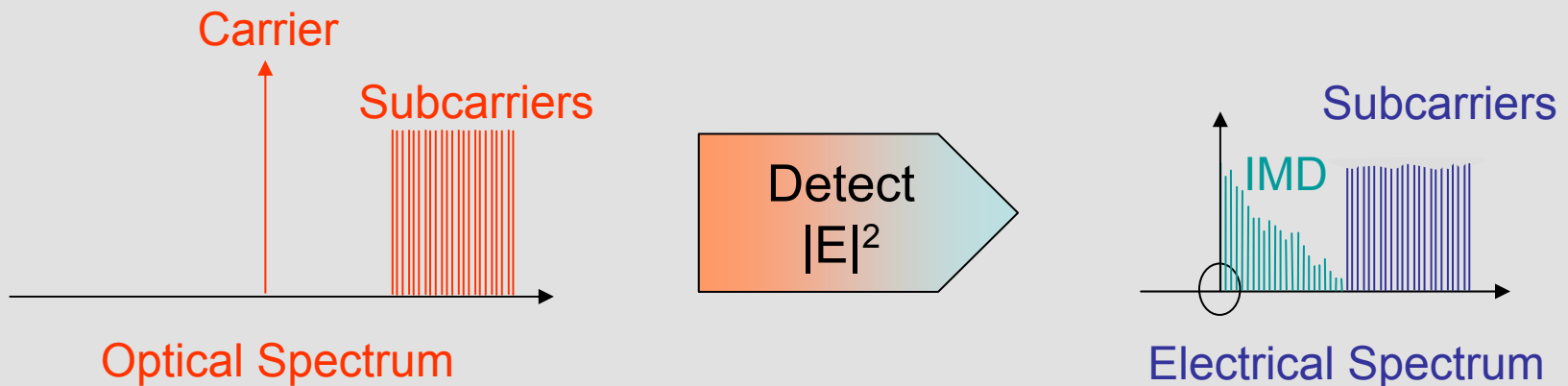


With Optical Single Sideband, there is only one photodetection component at each electrical frequency, so there is no nulling at certain frequencies.

The phase shift  $\theta_k$  due to dispersion can be equalised in the electrical domain.

# Why Frequency Band Offset?

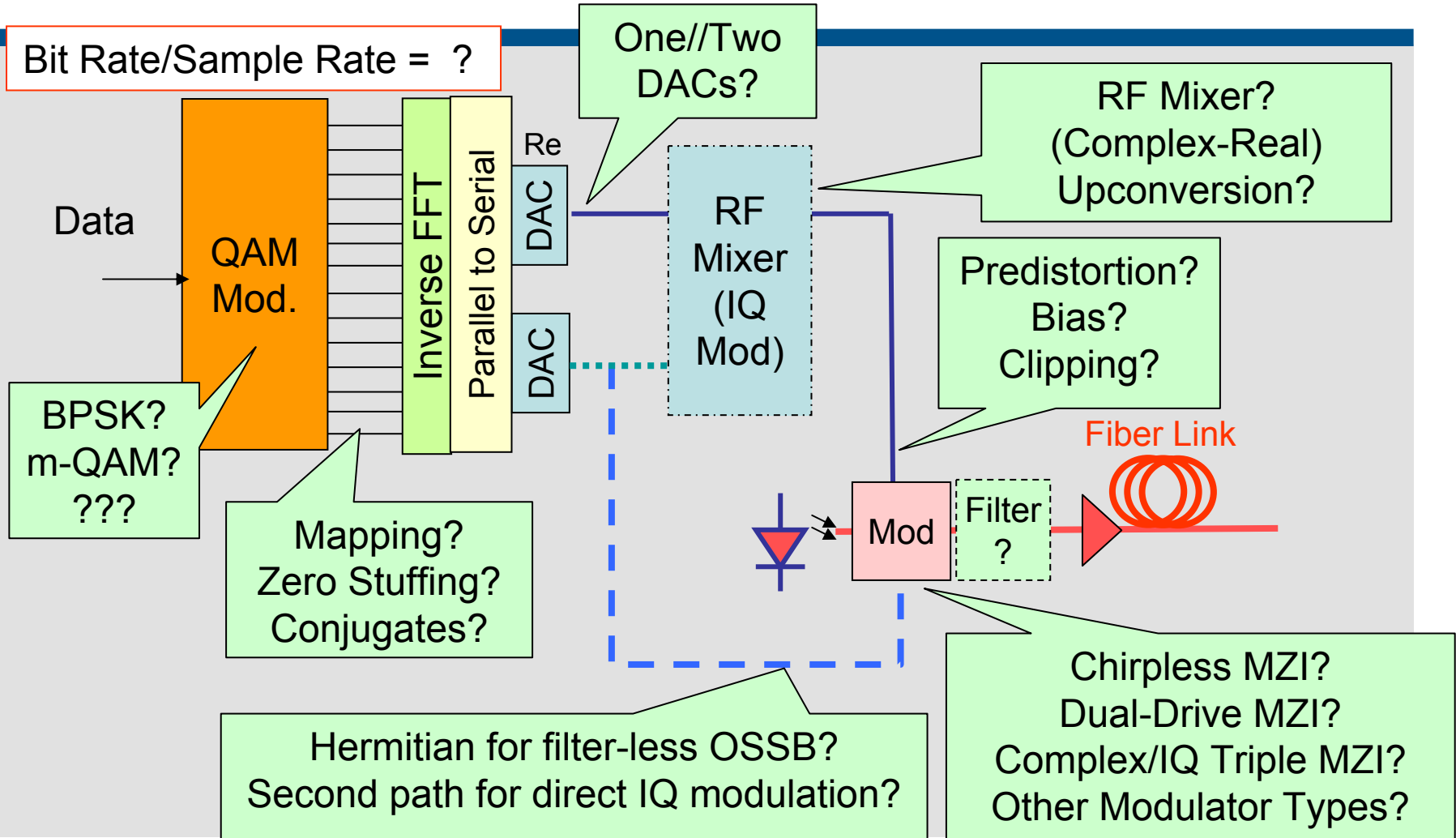
- Intermodulation distortion
  - Distortion due to *subcarrier* × *subcarrier* mixing
  - Signal due to *subcarrier* × *carrier* mixing



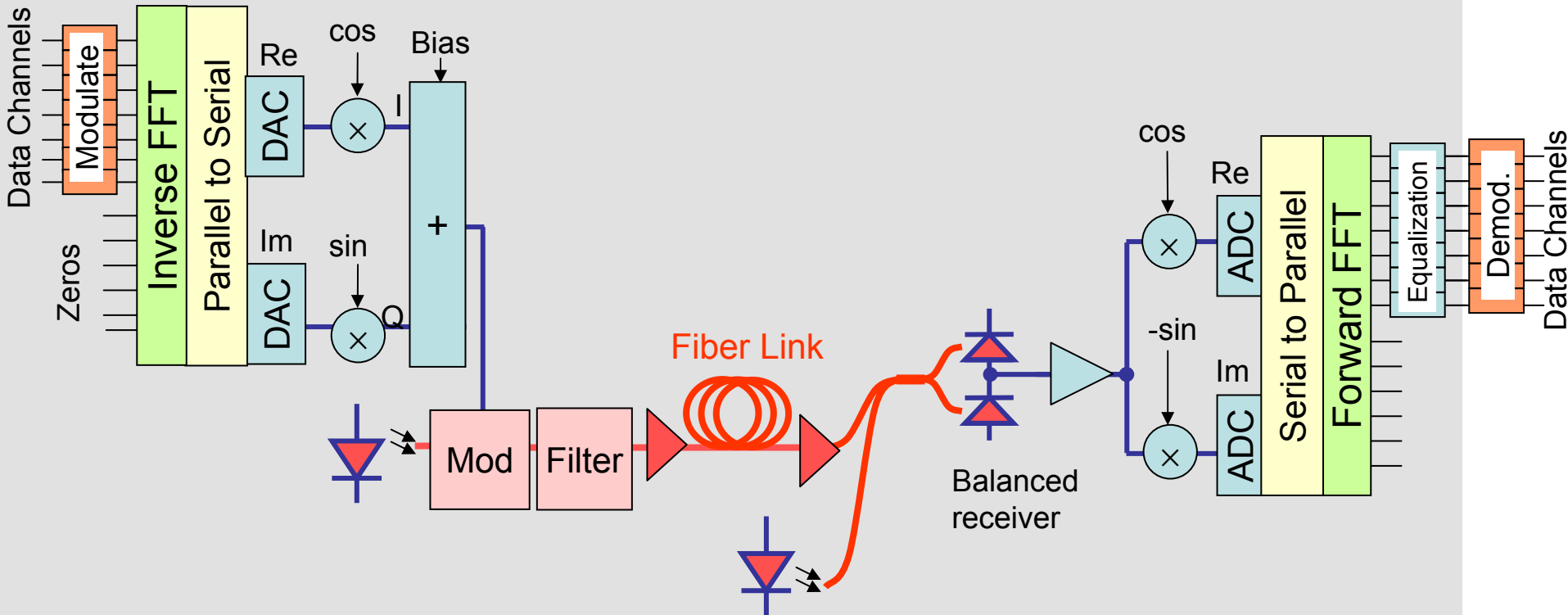
- Offsetting the subcarriers from the carrier means the distortion products will mainly fall outside OFDM band
  - Allows a highly-suppressed carrier

# Transmitter and Receiver Options

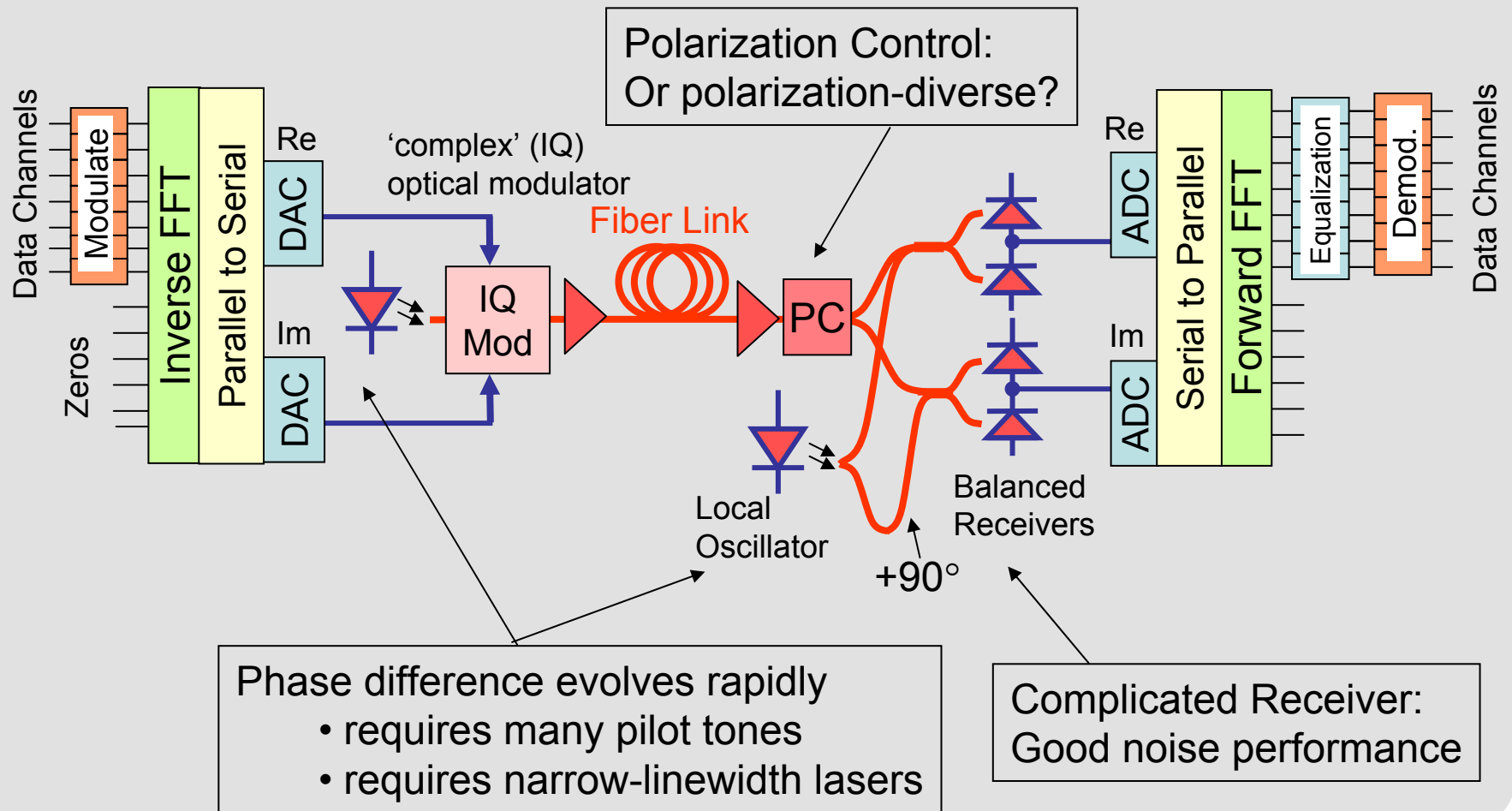
# Transmitter Choices



# Coherent System (RF upconversion, Heterodyne receiver)



# Coherent System (direct IQ modulation and homodyne detection)



# Experimental Results

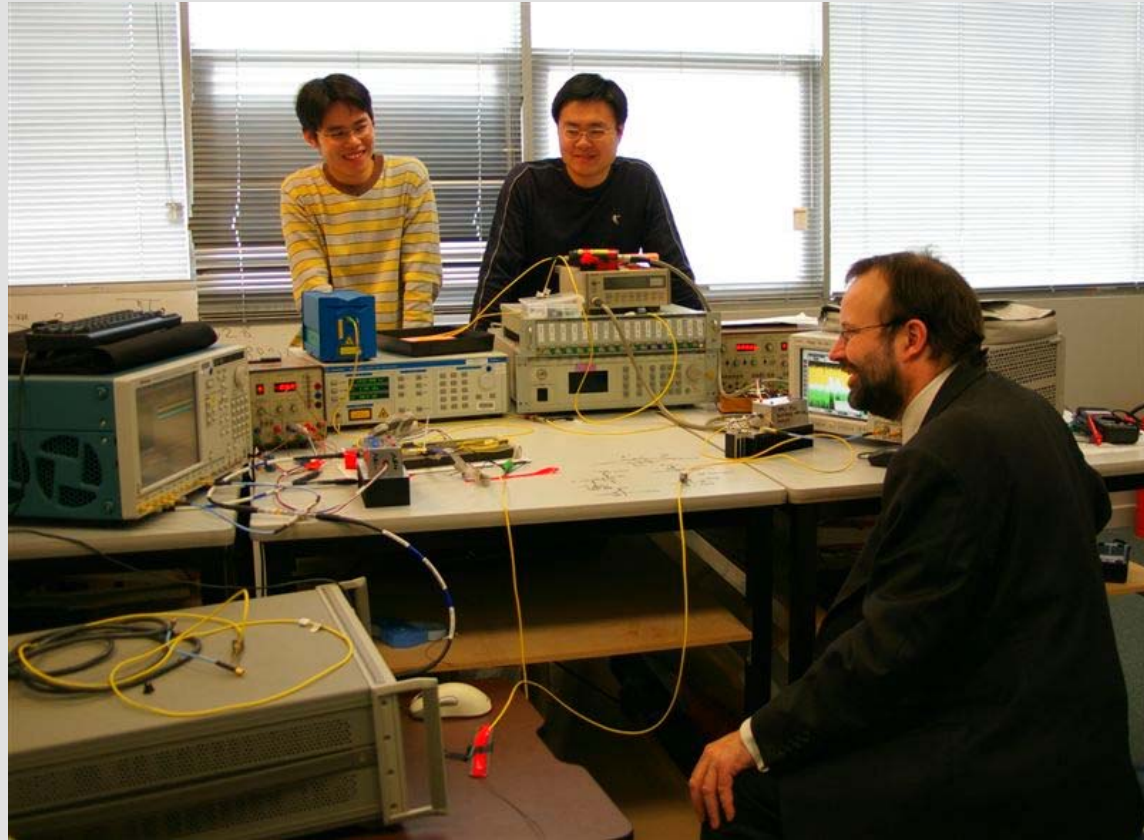
From Monash University

# Our Experimental Results (OFC2007 Post Deadline)

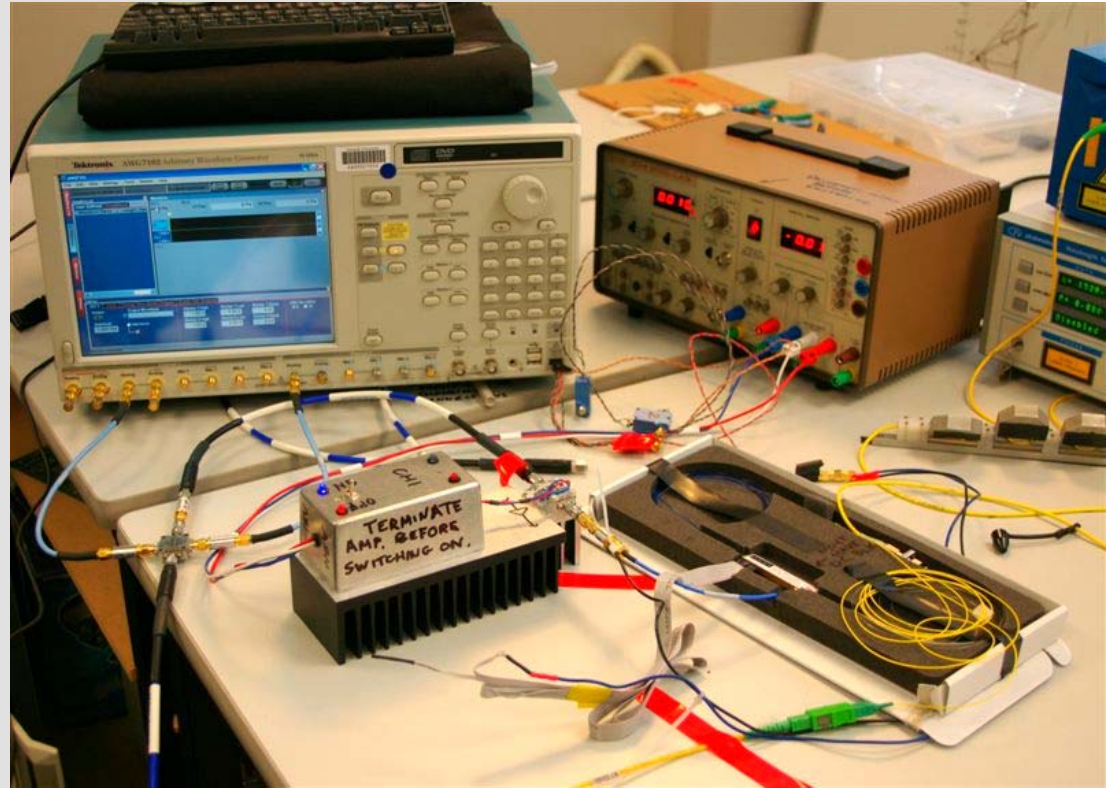
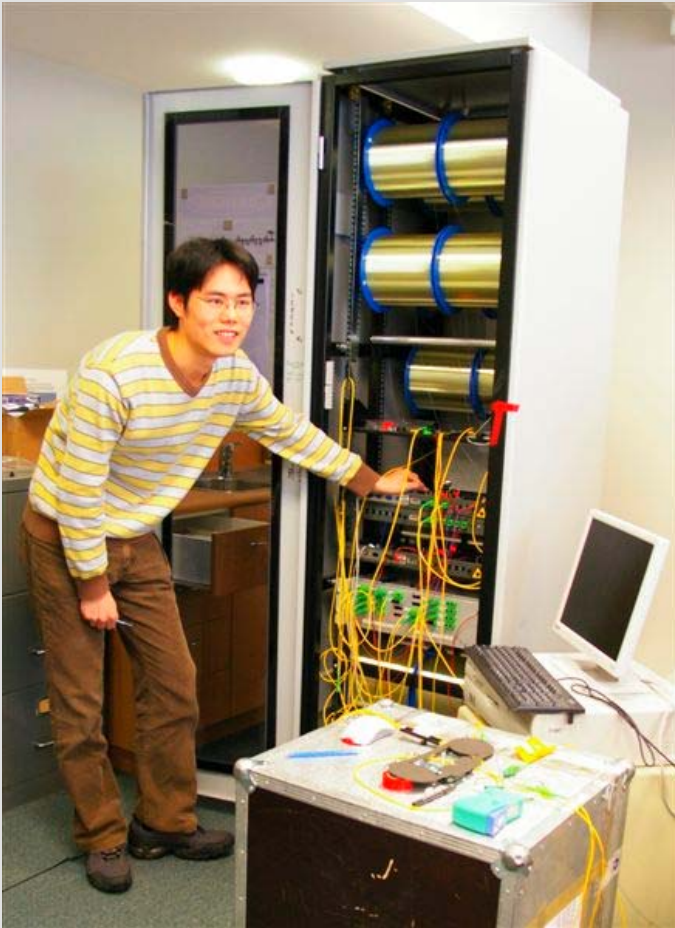
Rate	QAM	Length	Comments	BER
20 Gbit/s	16 QAM	320 km	Single DAC OSSB using filter	2.5e-3
12 Gbit/s	32 QAM	400 km	Dual DAC Colorless OSSB Transmitter	3e-4
10 Gbit/s	4 QAM	400 km	Dual DAC RF Up-converter plus filter	1e-4

Details in our OFC 2007 Post-Deadline paper (schmidt, Lowery, Armstrong)

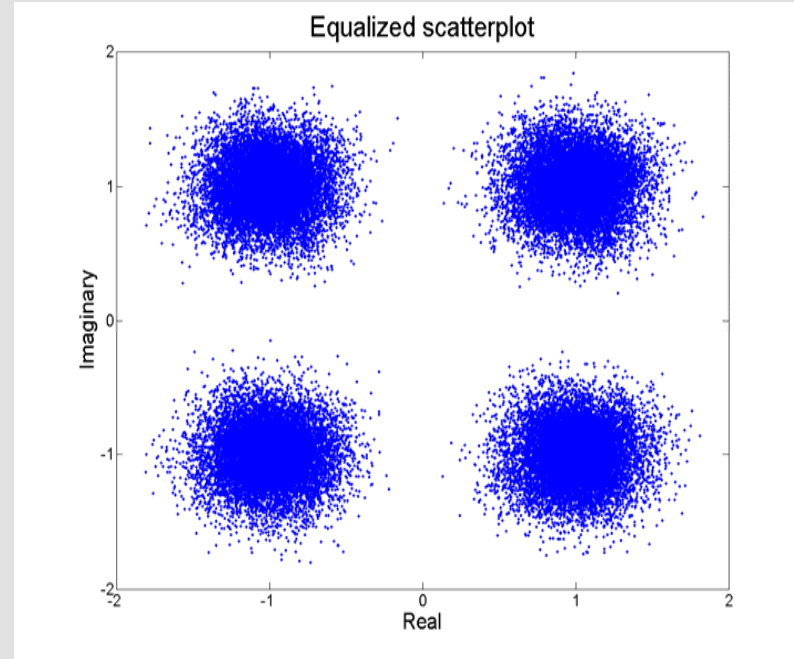
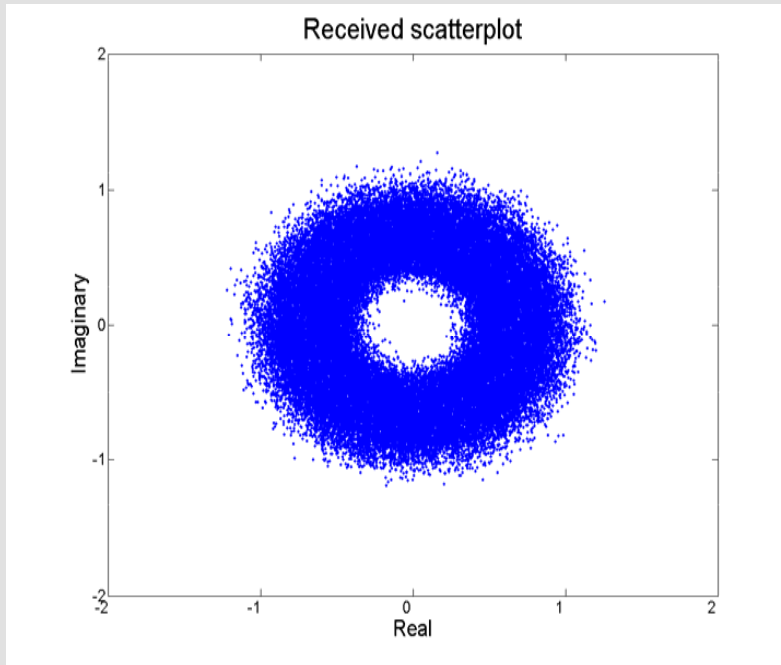
# Transmitter and Receiver



# Optical Link and Transmitter

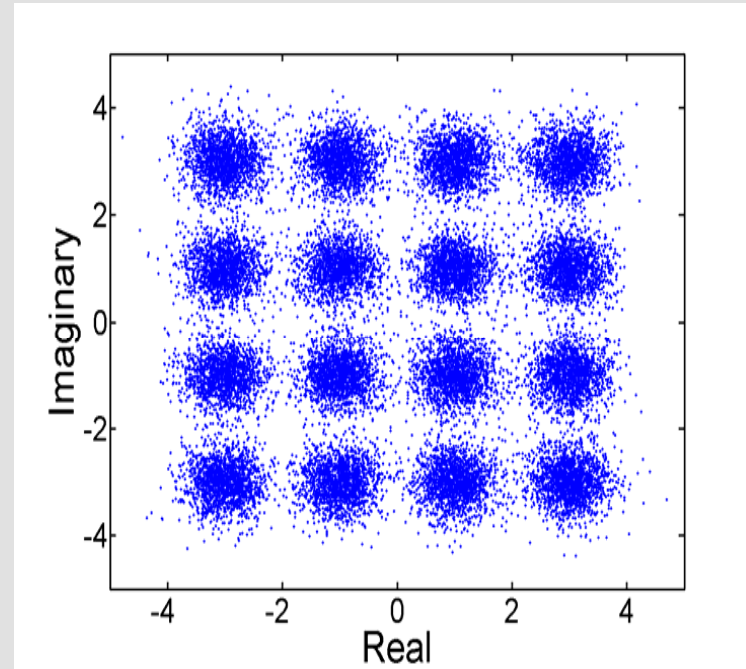
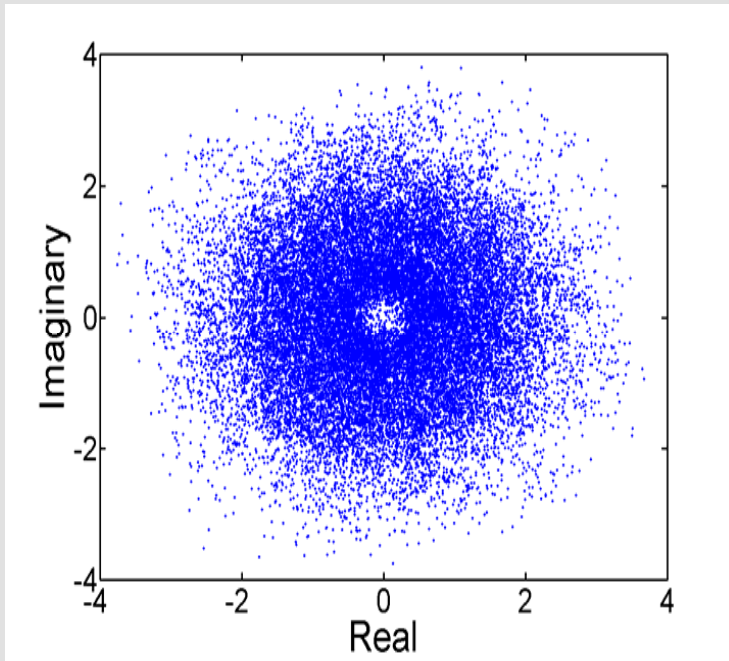


# 10 Gbit/s Using RF Mixers (400 km)



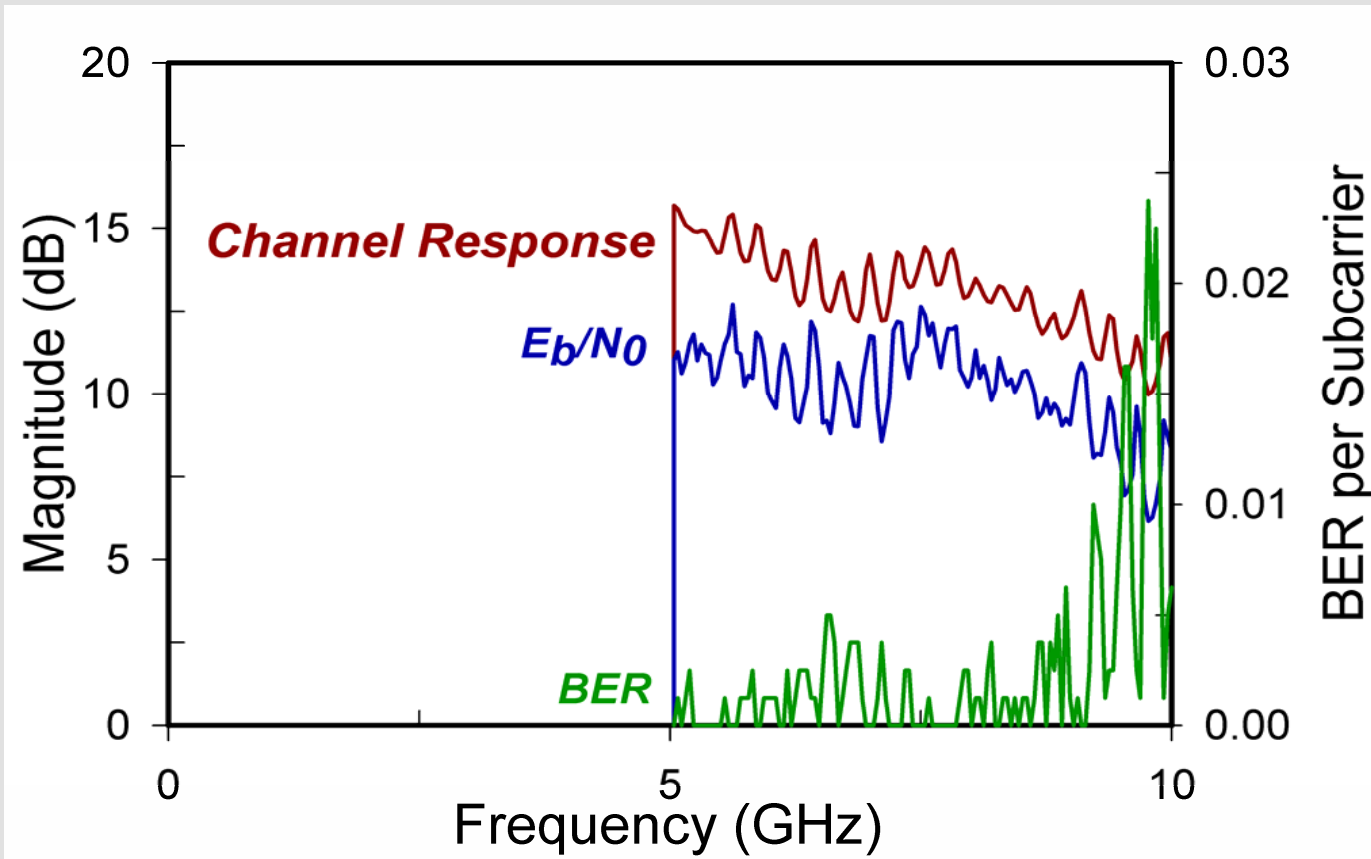
- 400km
- BER <  $10^{-5}$

# 20 Gbit/s Using Direct Digital Conversion



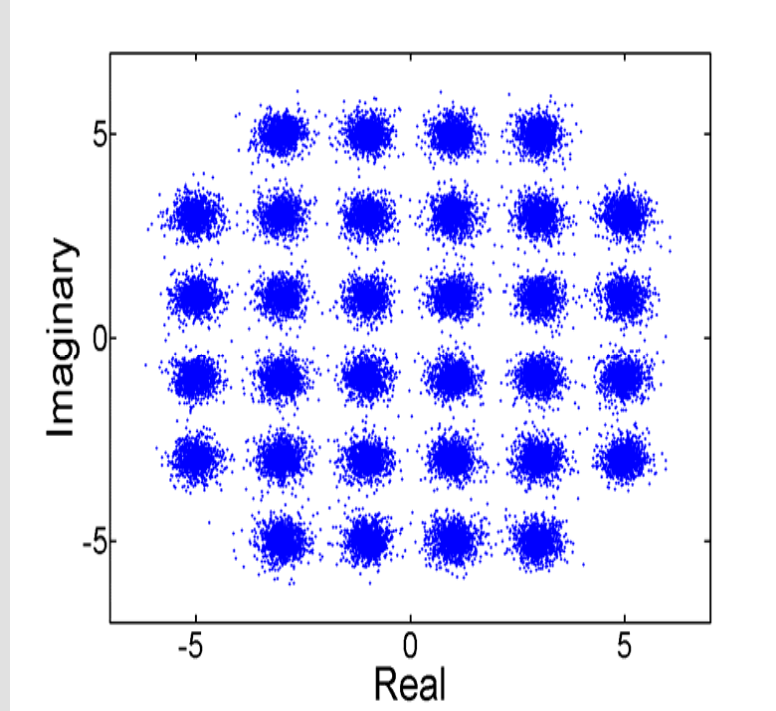
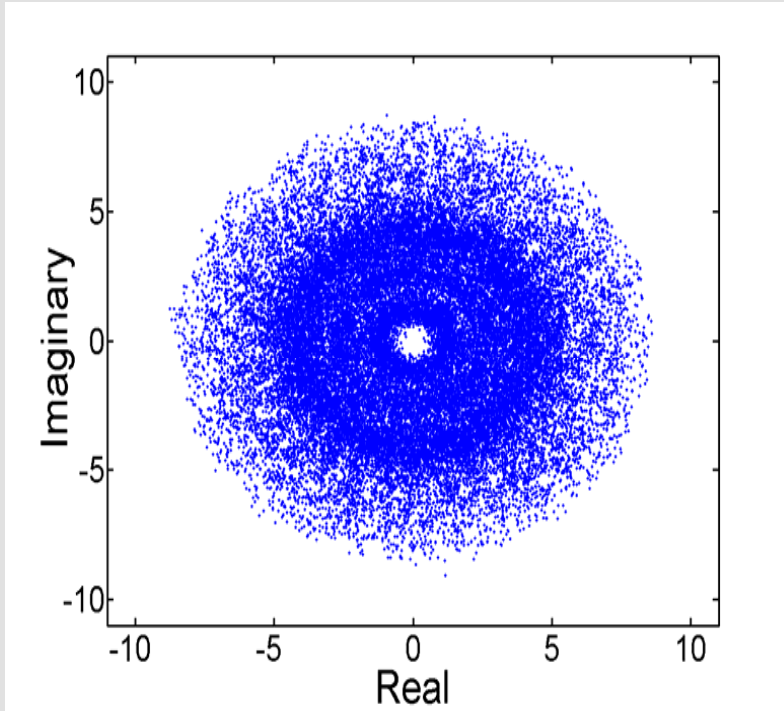
- 320 km
- $BER = 2.5 \times 10^{-3}$

# 20 Gbit/s Using Direct Digital Conversion



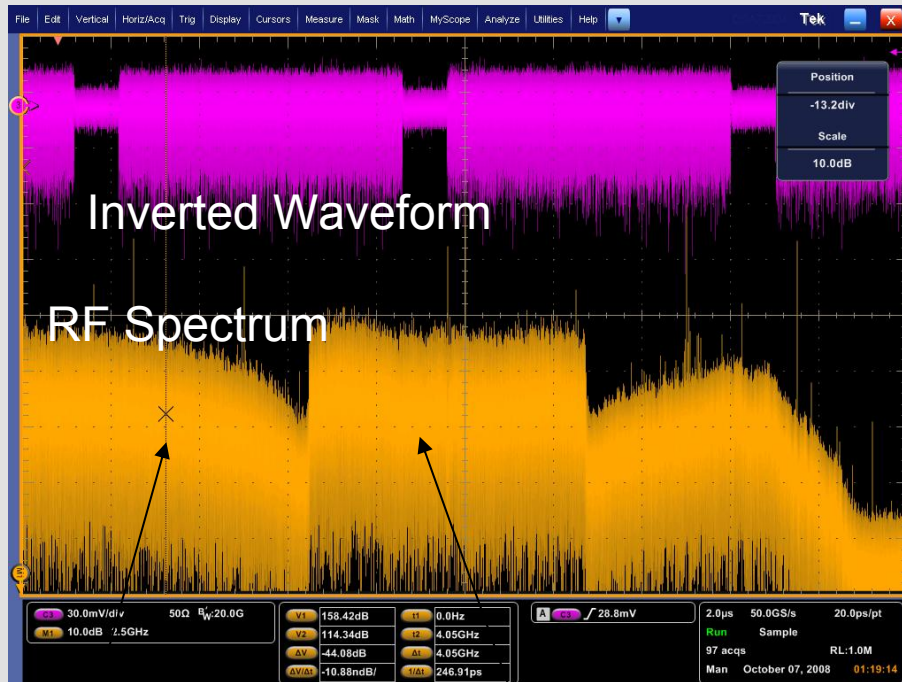
Channel response is a result of electrical and optical components.

# 12 Gbit/s Using Colorless Transmitter (2006)



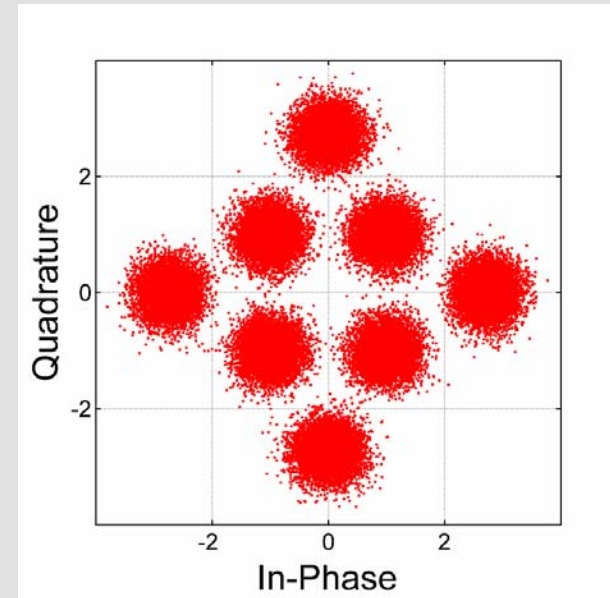
- 400km
- BER =  $3 \times 10^{-4}$  for 184,000 bits

# 24 Gbit/s Using Modified Colorless Transmitter (using only 10 GS/s DACs)



*Signal × Signal*

*Signal × Carrier*



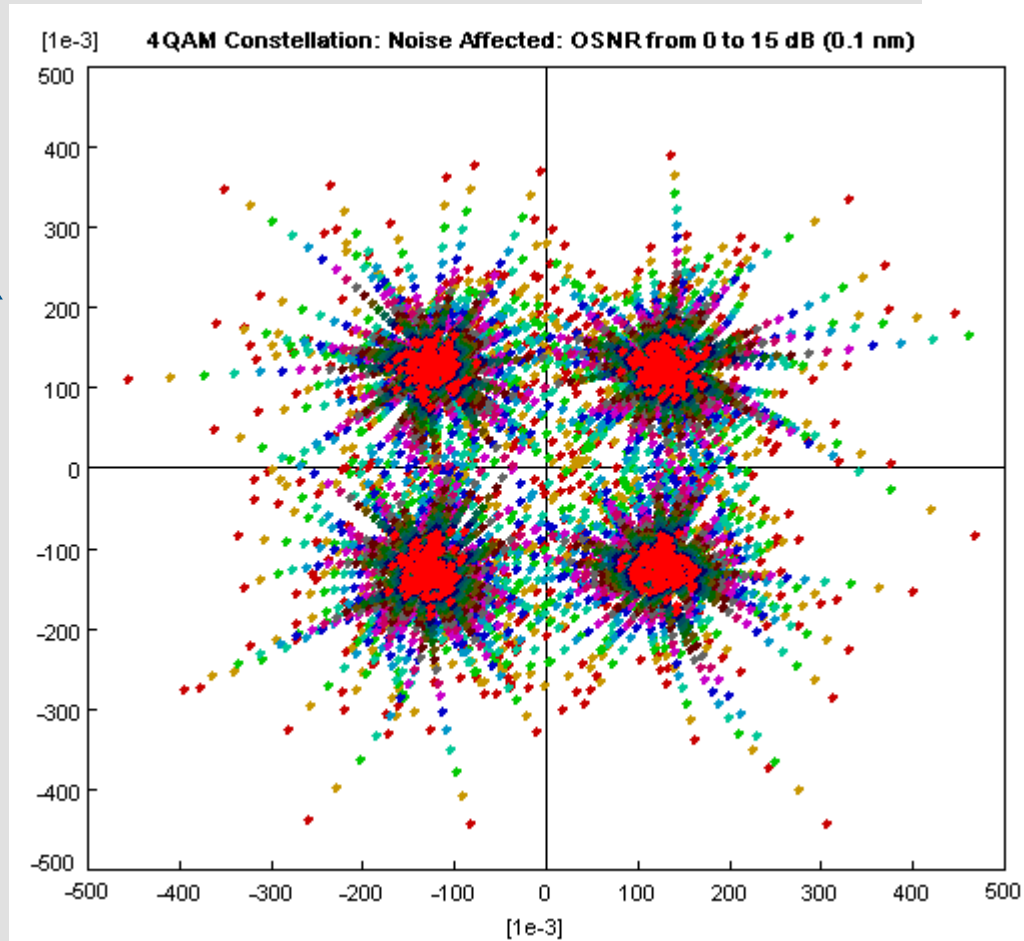
BER of  $2 \times 10^{-4}$   
(800 km, 40-GHz ASE filter)

# Impairments

## Amplified Spontaneous Emission

# Effect of Amplifier Noise (ASE)

- ASE causes bivariate Gaussian spreading of points
- This is a sweep of OSNR from 0 dB to 15 dB.
- The same random sequence is used for each noise level – radial spreading
- **Bright Red** is 15 dB OSNR



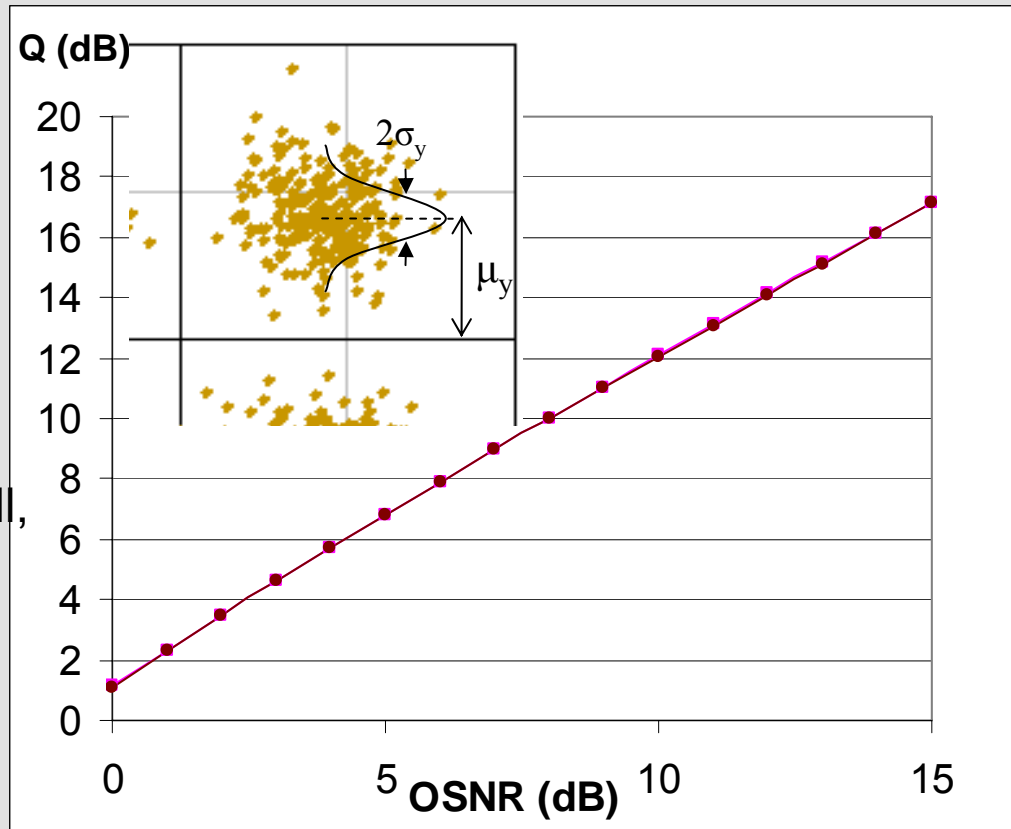
# Q versus OSNR

- $Q_{\text{dB}} = 20 \cdot \log_{10} q$
- $q = \sigma_x / \mu_x = \sigma_y / \mu_y$

For 4-QAM  
optimum filtering  
ASE dominated,  
modulator biased at quad. or null,  
 $P_{\text{carrier}} = P_{\text{sideband}}$

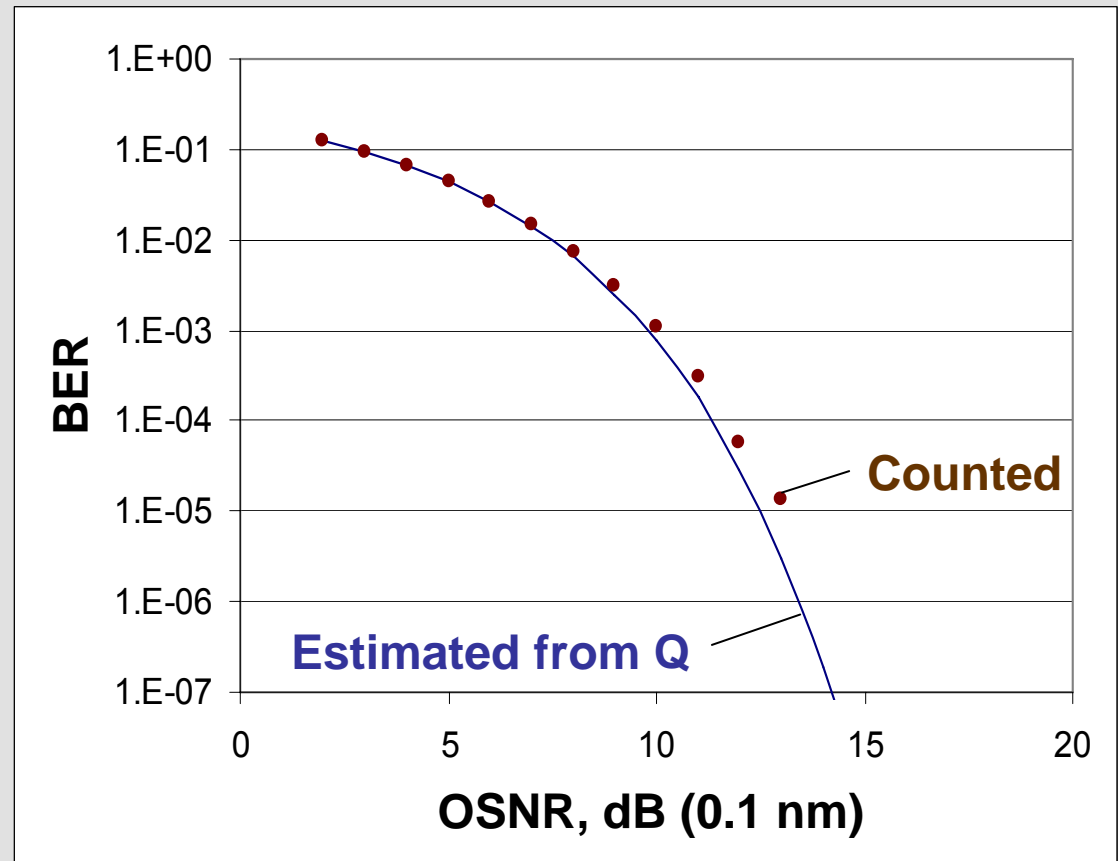
$$Q_{\text{dB}} = 1.0615 \text{ OSNR} + 1.4032 \text{ dB}$$

$$R^2 = 0.9994$$

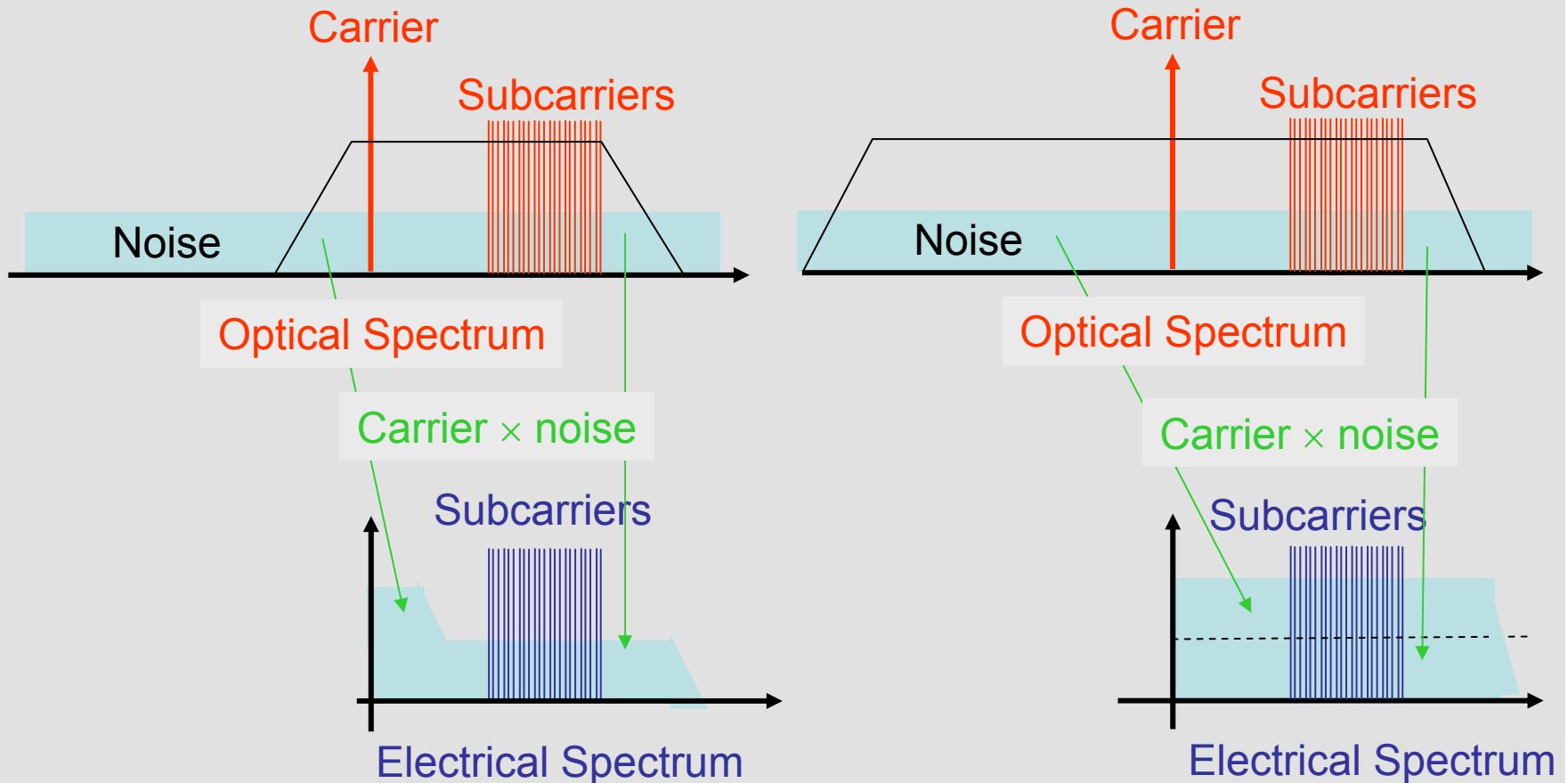


# BER versus OSNR

- BER(estimate)  
 $= \frac{1}{2} \text{erfc}(q/\sqrt{2})$
- erfc is Excel definition
- 10 dB OSNR gives 0.001 BER



# Effect of Filter Bandwidth: noise from image

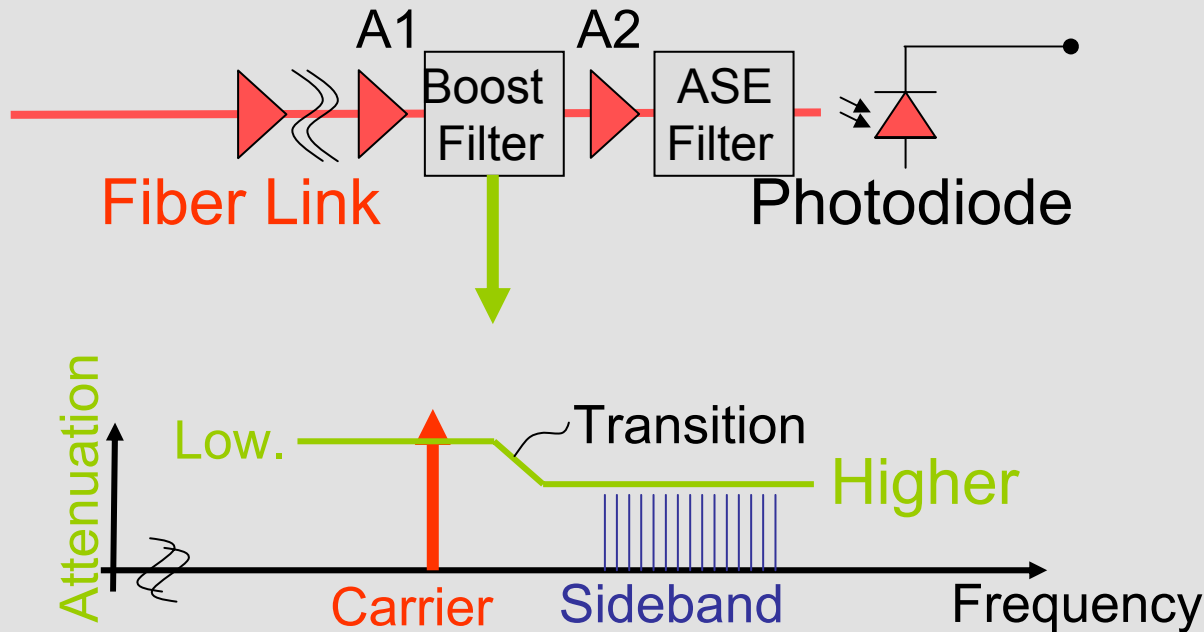


# Carrier Boost in DD-OFDM

One way of obtaining good performance is a **strong local oscillator** (compared with the signal):

suppresses:  $Signal \times Signal$ ,  $Signal \times ASE$ ,  $ASE \times ASE$ ,

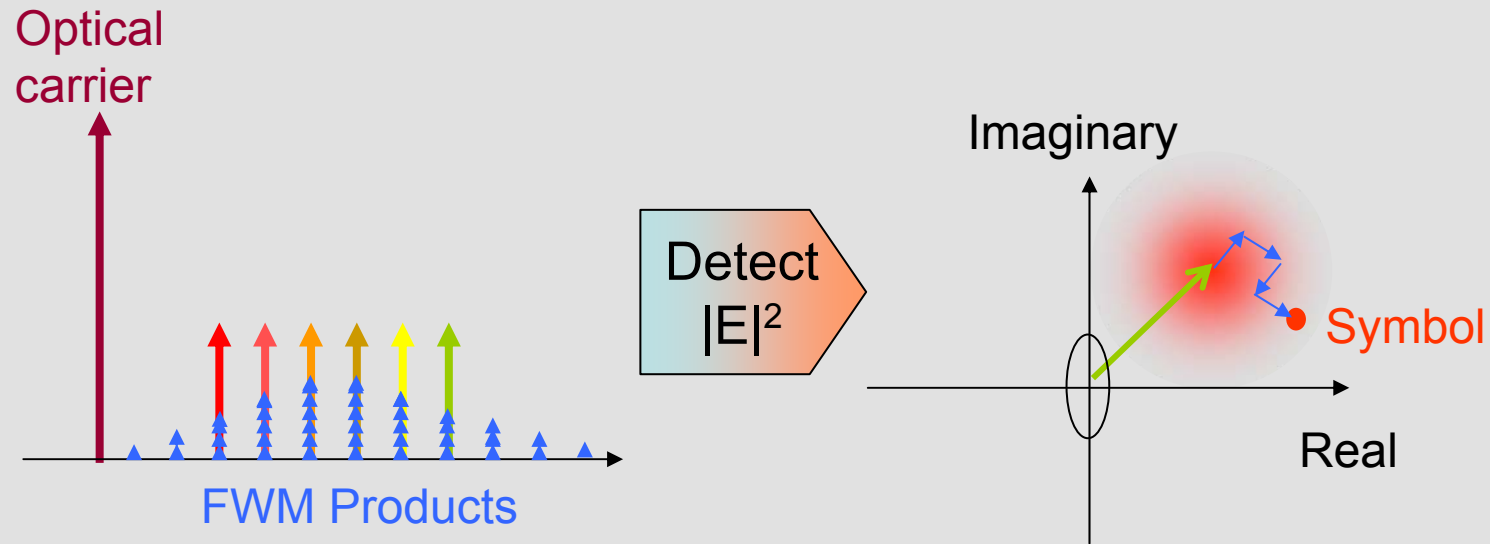
- so why not **boost** the carrier to mimic a strong local oscillator?



# Impairments

## Nonlinearity

# Effects of Nonlinearity – Theory



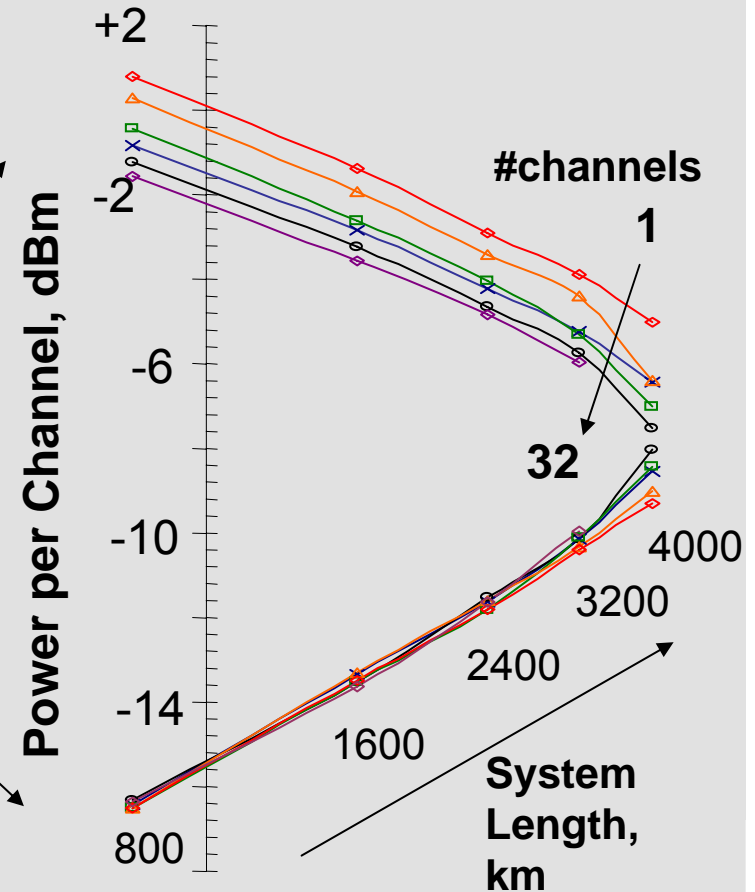
Close carriers mean strong FWM products (no 'walk-off')

**FWM products** have random, but distinct, phases. They add as a random walk to the **signal vector**, causing a **Gaussian spread**.

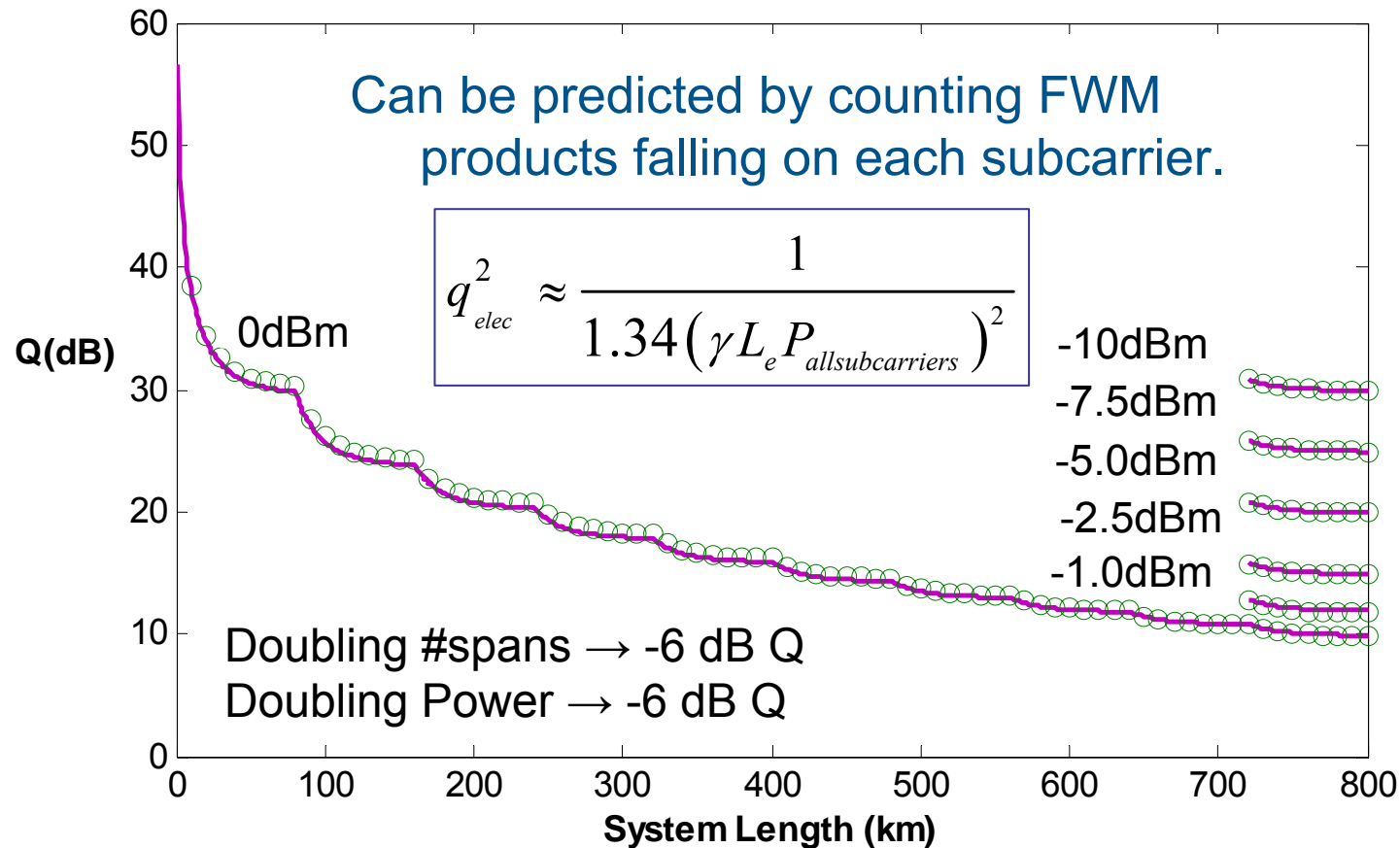
The FWM degradation is independent of the number of carriers.

# Effects of Nonlinearity – 80 km spans WDM

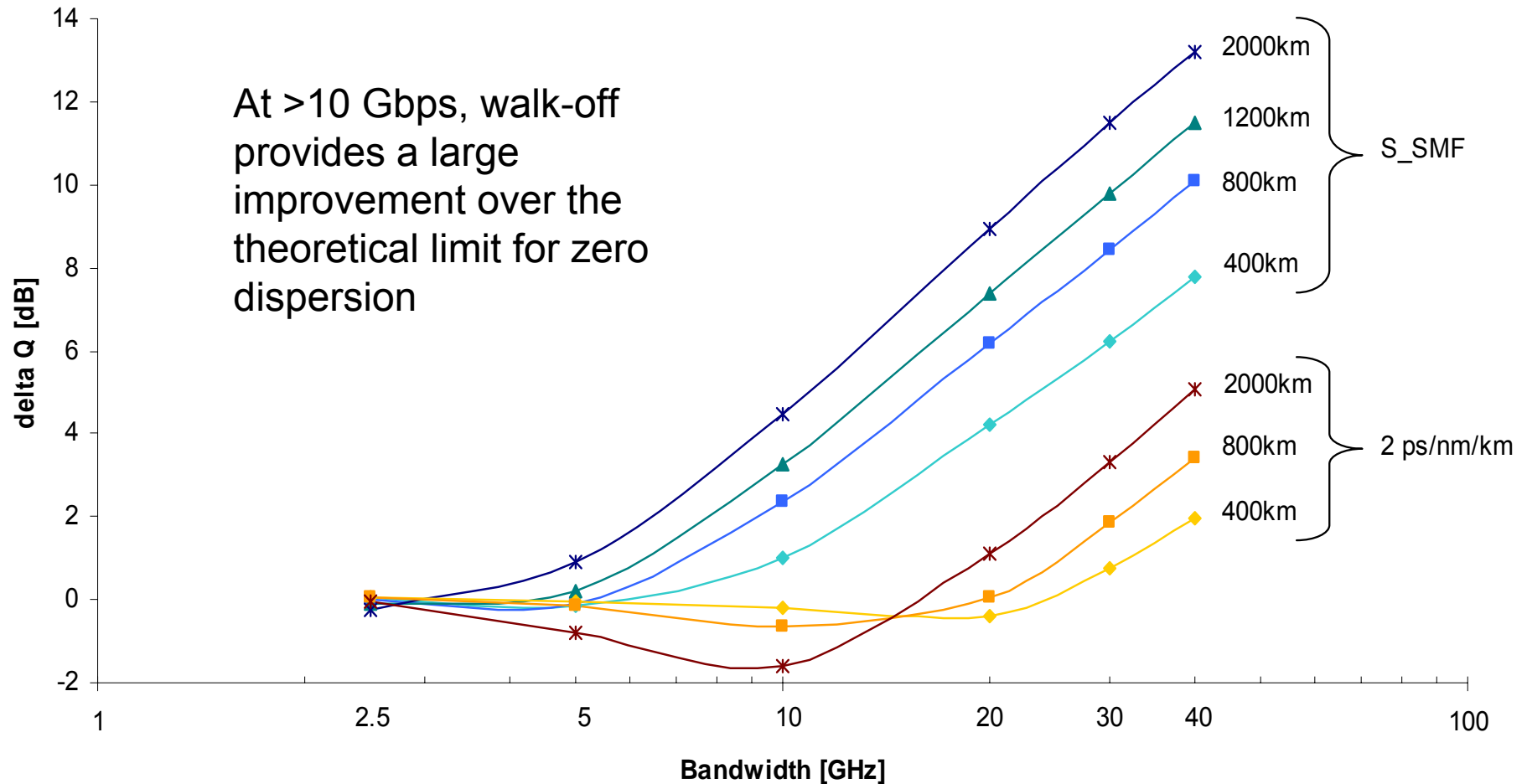
- Lines for  $Q = 11.4$  dB
- Nonlinearity affects max. power
  - Depends on channel count
- Noise affects min power
  - “58 equation”
- 5 dB decrease in margin per doubling of length



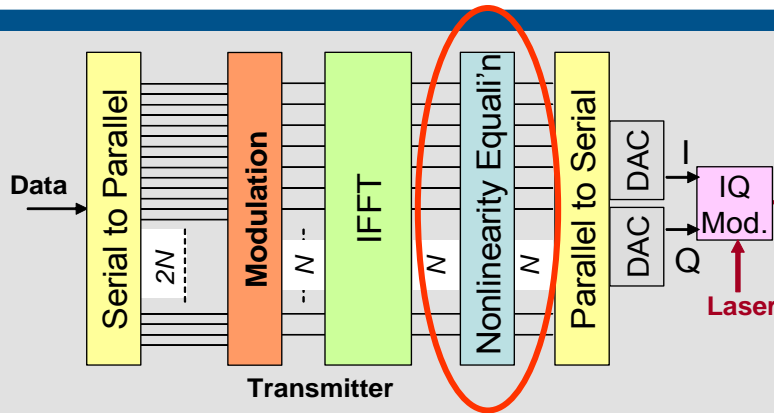
# Effects of Nonlinearity – Q limit with multiple 80 km spans WDM (coherent)



# Effect of Dispersion on Nonlinearity



# Nonlinearity Compensation

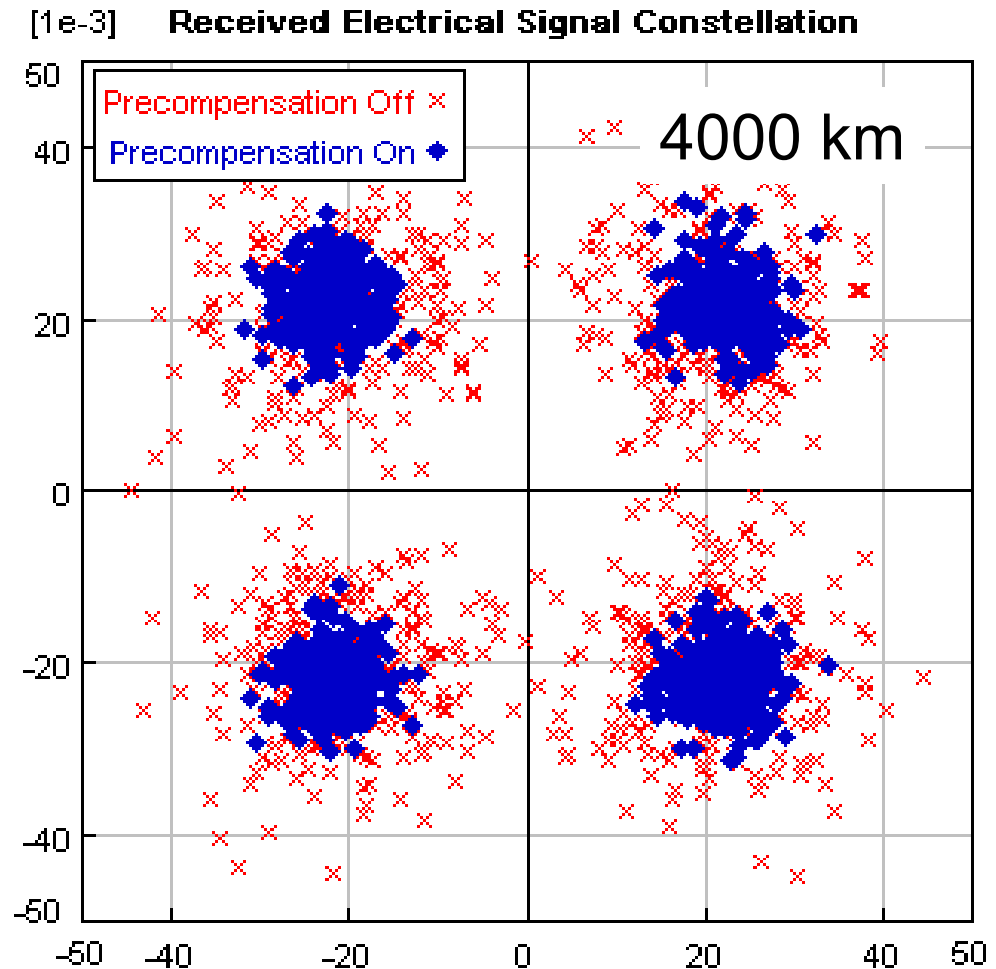


**Nonlinearity (t)**

Very simple implementation:

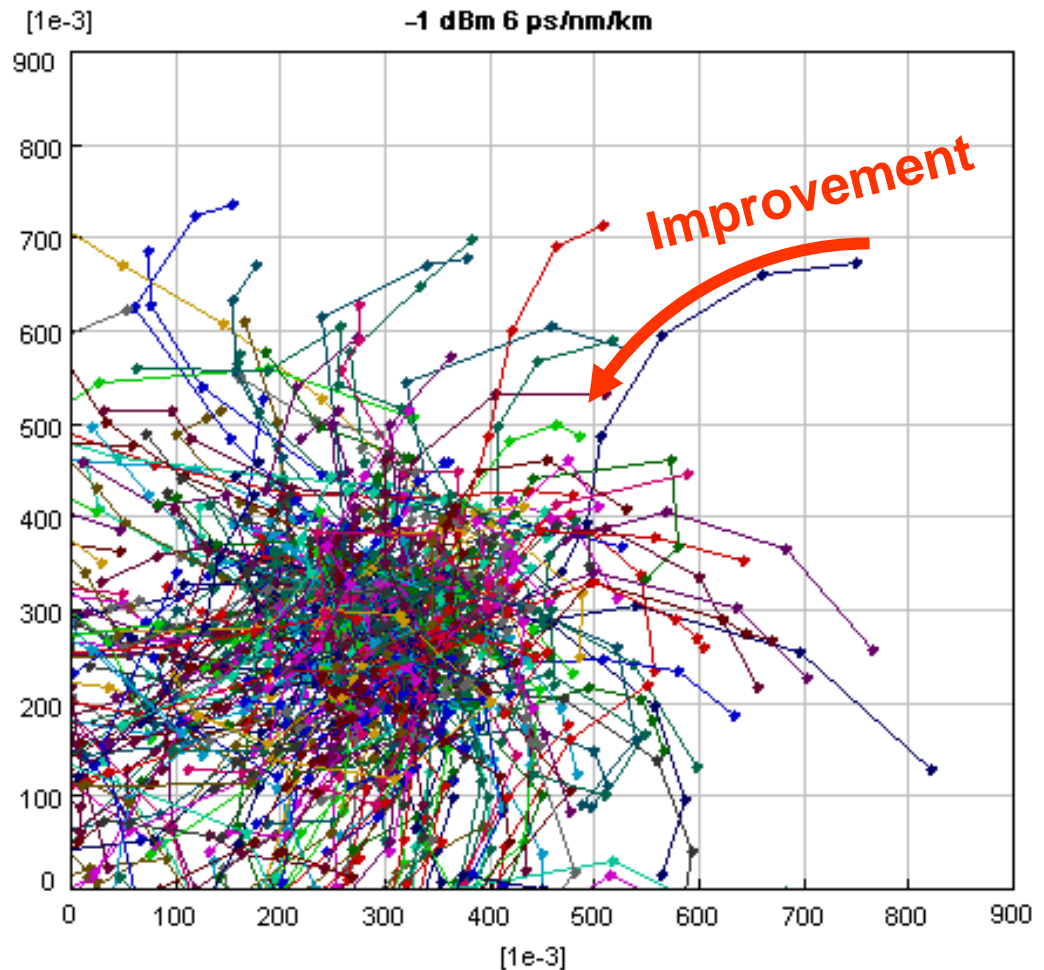
$$\theta(t) = P(t) \cdot sL_{eff} \cdot 2\pi n_2 / (\lambda_0 A_{eff})$$

Increase in Q is > 7 dB!

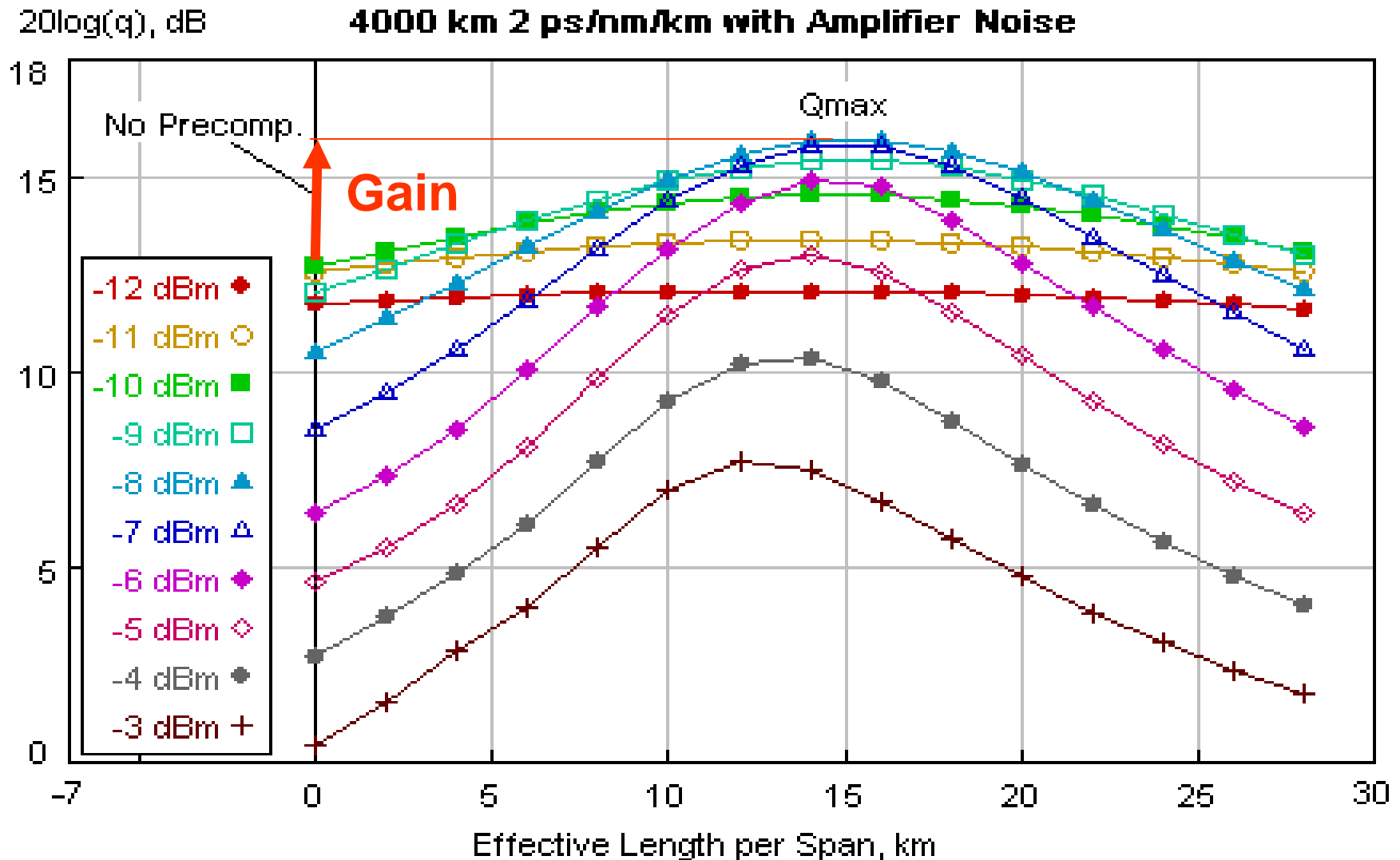


# Nonlinearity Compensation

- Nonlinearity compensation pulls-in outlying points of each subcarrier
- Walk off means the improvement is limited
  - But it is still useful!



# Nonlinearity Compensation



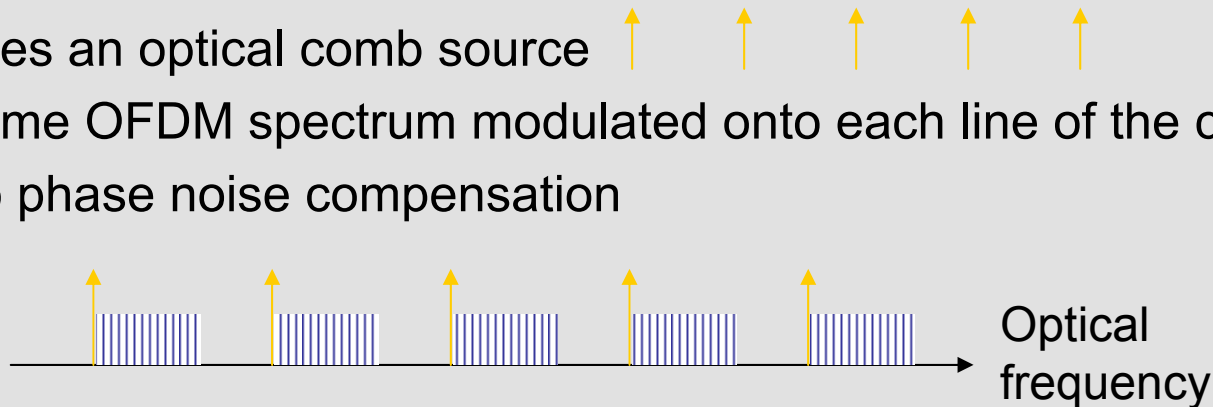
# Scaling OFDM to higher bit rates

- OFDM is numerically efficient
  - for 1000 km of fiber at 10 Gbit/s, MLSE requires 370× more than OFDM
  - And fewer than Pre/Post compensation (few times)

Henning Bülow: OMG5, OFC 2007

# 100G Systems Demonstrations

- *Sander Jansen et al.*
  - Uses dual-polarization transmission with electronic PMD compensation
  - Subcarriers contain a pilot tone to allow phase noise to be compensated in the RF domain
- *William Shieh et al.*
  - Uses an optical comb source
  - Same OFDM spectrum modulated onto each line of the comb
  - No phase noise compensation

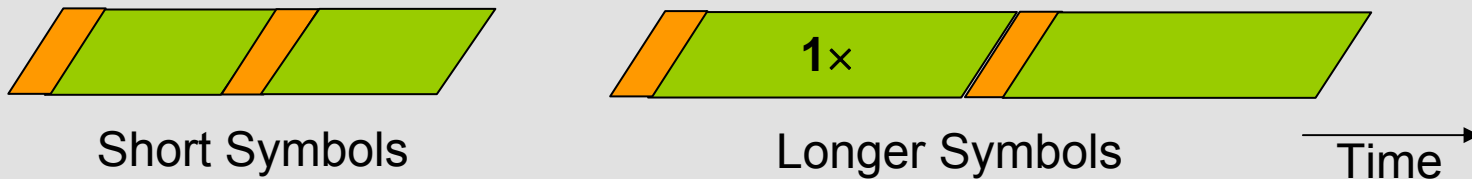


# Efficiency and scaling to higher bit rates

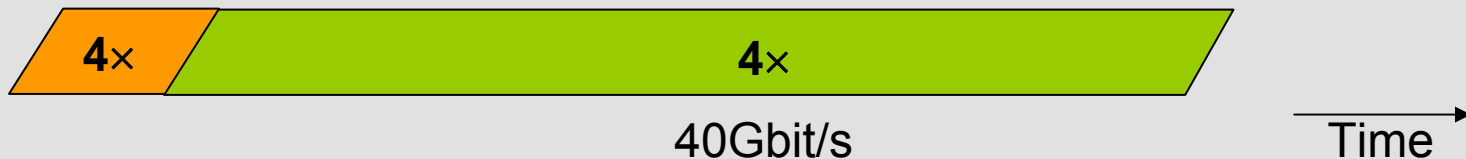
- OFDM is Scalable to higher bit rates
  - Processing complexity is prop. to  $5N \cdot \log_2(N) + k \cdot N$
  - With 4096 symbols, 40 Gbps requires 24× more processing per OFDM Symbol
  - But we have  $N \times$  more time to do it
    - > (4096 OFDM symbol covers 4 × more time at 40 Gbps)
  - So computation speed requirement is **only 6×** that of 10 Gbit/s

# Scaling to higher bit rates: Overhead

- Longer symbols ( $N$ ) add a proportionally shorter cyclic prefix – a lower overhead



- For 10% overhead at 4000 km, 10 Gbps,  $N=256$ 
  - Increases to  $N=4096$  at 40 Gbps (because of higher bandwidth of the optical signal and the higher bit rate, hence symbol rate)



# Conclusions

- Orthogonal Frequency Division Multiplexing offers advantages for long-haul dispersion compensation:
  - No reverse feedback path
    - > Responds to rapid fluctuations
  - Signal can be dropped at any point
  - Timing synchronization easy (no clock recovery)
  - Slower DACs and ADCs, especially if RF subcarrier is used
  - Self-monitoring
  - Compensates for electrical and optical channel imperfections
- We have shown 20 Gbit/s (all digital), 24 Gbit/s (colorless, all-digital) and 10 Gbit/s (RF mixers)
- More scalable than MLSE (and starts from a better base)
  - only 6× more processing for 40 Gbps

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